

task_wjttvmydrskzhcim_with_calculation

Student Group

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complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E9 Component Parameters
(written test, approx. 10 % of a 120-minute written test, SS2021)

Determine the complex impedance of a motor (motor presents a resistive inductive load) for the next exercises consider the following:
 The RMS values of the series resistance R_{M} and the inductance L_{M} are to be determined below. Both results in the impedance of the motor.
 For two different frequencies, the rms values of the applied voltage U_1 and U_2 was applied.

This resulted in the recorded current of
 a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|Z| = \sqrt{(2\pi f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = \frac{U_1}{I_1} - 2\pi f_1 L_{\text{M}}$$

$$L_{\text{M}} = \frac{U_2}{I_2} - \frac{R_{\text{M}}}{2\pi f_2}$$

b) Since we have the absolute values of the impedances from the specified formulas from a) and this has the advantage that R_{M} will cancel out:

$$Z_2^2 - Z_1^2 = (2\pi f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

$$\underline{Z_2^2 - Z_1^2 = (2\pi)^2 \cdot L_{\text{M}}^2 \cdot (f_2^2 - f_1^2)}$$

The complex impedance \underline{Z} for a resistive inductive load R_{M} and L_{M} in series circuit is given as $\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$

$$|Z| = \sqrt{R_{\text{M}}^2 + (\omega L_{\text{M}})^2}$$

Now we can rearrange to L_{M} :
 The Pythagorean theorem can derive the absolute value:

$$|Z_2|^2 - |Z_1|^2 = (2\pi f_2 L_{\text{M}})^2 + R_{\text{M}}^2 - ((2\pi f_1 L_{\text{M}})^2 + R_{\text{M}}^2)$$

$$\underline{|Z_2|^2 - |Z_1|^2 = (2\pi)^2 \cdot L_{\text{M}}^2 \cdot (f_2^2 - f_1^2)}$$

$$L_{\text{M}} = \frac{\sqrt{|Z_2|^2 - |Z_1|^2}}{(2\pi)^2 \cdot (f_2^2 - f_1^2)}$$

$$L_{\text{M}} = \frac{\sqrt{50^2 - 40^2}}{(2\pi)^2 \cdot (100^2 - 50^2)}$$

$$L_{\text{M}} = \frac{\sqrt{900}}{4\pi^2 \cdot 7500} = \frac{30}{4\pi^2 \cdot 7500} = \frac{1}{1000\pi^2} \text{ H}$$

$$L_{\text{M}} = \frac{1}{1000 \cdot 9.8696} = 1.0132 \cdot 10^{-5} \text{ H} = 10.132 \mu\text{H}$$

And then to R_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{|Z_2|^2 - |Z_1|^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10\Omega)^2 - (6.25\Omega)^2}{100^2 - 50^2}} = 14.346 \mu\text{H}$$

The resistance value R_{M} can be derived from $Z_2^2 = (2\pi f_2 L_{\text{M}})^2 + R_{\text{M}}^2$
 $R_{\text{M}}^2 = Z_2^2 - (2\pi f_2 L_{\text{M}})^2$
 $R_{\text{M}} = \sqrt{Z_2^2 - (2\pi f_2 L_{\text{M}})^2}$

$$R_{\text{M}} = \sqrt{(10\Omega)^2 - (2\pi \cdot 100 \cdot 1.0132 \cdot 10^{-5} \text{ H})^2} = 4.3301 \Omega$$

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