

task_7el8zljglaazxtw_with_calculation

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exercise E13 Series Resonant Circuit (written test, approx. 10 % of a 120-minute written test, SS2022) 2

resonant circuit, exam ee2 SS2022

Exercise E13 Series Resonant Circuit
(written test, approx. 10 % of a 120-minute written test, SS2022)

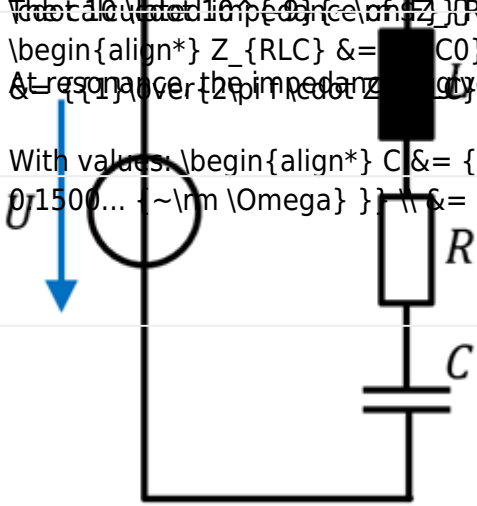
2. What is the resonance frequency of a series RLC circuit with an inductor of inductance L and a capacitor of capacitance C in series? The resonance frequency is the frequency at which the impedance of the circuit is purely resistive.

At this frequency, the inductive reactance X_L and the capacitive reactance X_C are equal in magnitude and opposite in phase, so they cancel each other out. The total impedance Z_{RLC} is then equal to the resistance R .
 Which value would C have for the given f_0 ?

- Path: $C = 10 \text{ nF}$
- $R = 100 \text{ } \Omega$
 - $Z_{RLC} = 250.5 \text{ } \Omega$
 - $L = 60 \text{ } \mu\text{H}$
 - $R = 10 \text{ } \Omega$

The resonance frequency is given as $f_r = \frac{1}{2\pi\sqrt{LC}}$
 $\frac{1}{2\pi\sqrt{LC}} = 100 \text{ MHz}$
 $\frac{1}{2\pi\sqrt{60 \cdot 10^{-12} \cdot C}} = 100 \text{ MHz}$
 $Z_{RLC} = R = 100 \text{ } \Omega$
 At resonance, the impedance is purely resistive.

With values: $C = \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 100} = 10.6 \text{ nF}$



1. What is the impedance Z_{RLC} of this real capacitor for $f_0 = 100 \text{ MHz}$? (Phase and magnitude)

Path

The impedance Z_{RLC} is given by: $Z_{RLC} = R + j\omega L - \frac{j}{\omega C}$
 $Z_{RLC} = R + j\omega L - \frac{j}{\omega C}$

Putting in the numbers, only for the reactive part X_{LC} :
 $X_{LC} = 2\pi \cdot 100 \cdot 10^6 \cdot 60 \cdot 10^{-12} - \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 10 \cdot 10^{-9}}$
 $X_{LC} = -121.45 \text{ m}\Omega$

With the real and imaginary parts, we can derive the magnitude and phase:

$$Z_{RLC} = \sqrt{R^2 + X_{LC}^2} \quad \text{and} \quad \sqrt{(88 \text{ m}\Omega)^2 + (-121.45 \text{ m}\Omega)^2} = 150.0... \text{ m}\Omega$$

$$\varphi = \arctan\left(\frac{X_{LC}}{R}\right) = \arctan\left(\frac{-121.45 \text{ m}\Omega}{88 \text{ m}\Omega}\right) = -0.9437... = -54.07...^\circ$$

From:

<https://wiki.mexle.org/> - MEXLE Wiki

Permanent link:

https://wiki.mexle.org/electrical_engineering_and_electronics/task_7el8zljglaazxtw_with_calculation

Last update: **2024/07/05 02:21**

