

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

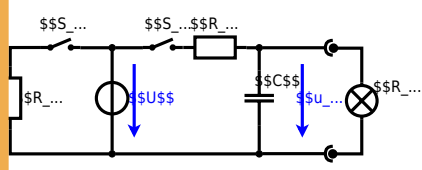
Exercise E9 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is open and the voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

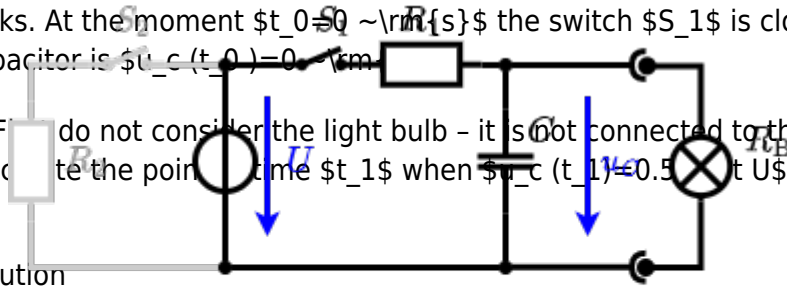
Solution: The internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



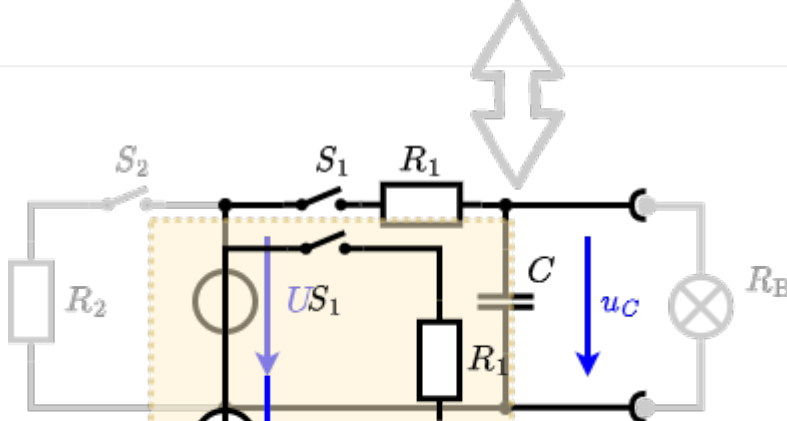
The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution



So, here only U and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ } \Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10 \text{ } \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ } \Omega \cdot 100 \text{ } \mu\text{F})})$$

Exercise E13 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC circuit with resistor values $R_1 = 1 \text{ } \Omega$ and $R_2 = 1 \text{ } \Omega$, and a capacitor with $C = 1 \text{ } \mu\text{F}$ is shown in the following circuit (of 3 S). $U = 1 \text{ V}$.
 Result: $f_1 = 20 \text{ kHz}$, $f_2 = 450 \text{ kHz}$. High frequencies are scarce. $I_1 = 50 \text{ mA}$ through R_1 .
 A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on every component.

$$R_{eq} = R_1 + R_2 + R_3 = 10 + 30 + 30 = 70 \Omega$$

The current is given by:

$$I = \frac{U}{R_{eq}} = \frac{50}{70} = 0.714 \text{ A}$$

The voltage across the capacitor is:

$$U_C = I \cdot X_C = 0.714 \cdot \frac{1}{\omega C} = 0.714 \cdot \frac{1}{100 \cdot 10^{-6}} = 7.14 \text{ V}$$

The voltage across the inductor is:

$$U_L = I \cdot X_L = 0.714 \cdot \omega L = 0.714 \cdot 100 \cdot 0.05 = 3.57 \text{ V}$$

The voltage across the resistor is:

$$U_R = I \cdot R = 0.714 \cdot 70 = 50 \text{ V}$$

The phase angle is given by:

$$\varphi = \arctan\left(\frac{X_L - X_C}{R}\right) = \arctan\left(\frac{3.57 - 7.14}{70}\right) = -2.86^\circ$$

The power factor is:

$$\cos(\varphi) = \cos(-2.86^\circ) = 0.999$$

The real power is:

$$P = U \cdot I \cdot \cos(\varphi) = 50 \cdot 0.714 \cdot 0.999 = 35.7 \text{ W}$$

The reactive power is:

$$Q = U \cdot I \cdot \sin(\varphi) = 50 \cdot 0.714 \cdot \sin(-2.86^\circ) = -3.57 \text{ var}$$

The complex power is:

$$S = P + jQ = 35.7 - j3.57 \text{ VA}$$

Exercise E11 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle and the real power (in W) of a series RLC circuit with the components (\$R\$ and \$X_L\$) shall be given.

After analysis, the following information can be extracted and given in phase (in \$Z\$):

$$Z = 10 + j20 - j40 = 10 - j20 \Omega$$

Solution

1. Calculation of the real values of the components.

Solution

$$R = 10 \Omega$$

$$X_L = \omega L = 100 \cdot 0.2 = 20 \Omega$$

$$X_C = \frac{1}{\omega C} = \frac{1}{100 \cdot 0.0005} = 20 \Omega$$

Solution

$$Z = R + jX_L - jX_C = 10 + j20 - j20 = 10 \Omega$$

The current is given by:

$$I = \frac{U}{Z} = \frac{50}{10} = 5 \text{ A}$$

The voltage across the resistor is:

$$U_R = I \cdot R = 5 \cdot 10 = 50 \text{ V}$$

The voltage across the inductor is:

$$U_L = I \cdot X_L = 5 \cdot 20 = 100 \text{ V}$$

The voltage across the capacitor is:

$$U_C = I \cdot X_C = 5 \cdot 20 = 100 \text{ V}$$

The phase angle is given by:

$$\varphi = \arctan\left(\frac{X_L - X_C}{R}\right) = \arctan\left(\frac{20 - 20}{10}\right) = 0^\circ$$

The real power is:

$$P = U \cdot I \cdot \cos(\varphi) = 50 \cdot 5 \cdot \cos(0^\circ) = 250 \text{ W}$$

The reactive power is:

$$Q = U \cdot I \cdot \sin(\varphi) = 50 \cdot 5 \cdot \sin(0^\circ) = 0 \text{ var}$$

The complex power is:

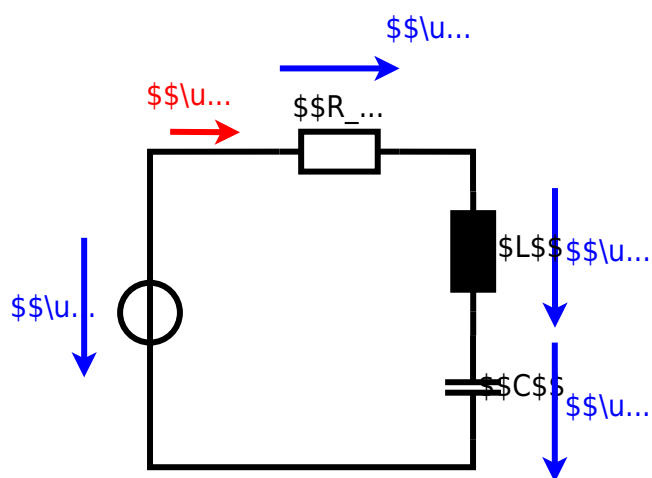
$$S = P + jQ = 250 + j0 \text{ VA}$$

With the complex part comes the phase angle \$\varphi\$:

$$\varphi = \arctan\left(\frac{X_L - X_C}{R}\right) = \arctan\left(\frac{20 - 20}{10}\right) = 0^\circ$$

The phase angle can be calculated as:

$$\varphi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-20}{10}\right) = -63.4^\circ$$



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