

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

Exercise E1 Charging Capacitors

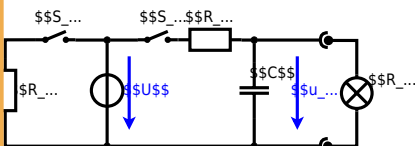
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the algebra) is in the slide of the 2019 exam. The circuit consists of a voltage source U and a resistor R_1 in series. This combination is connected to a parallel combination of a resistor R_2 and a capacitor C . The voltage across the capacitor is again U at the moment $t_0 = 0$ s when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1$ ms after closing the switch.

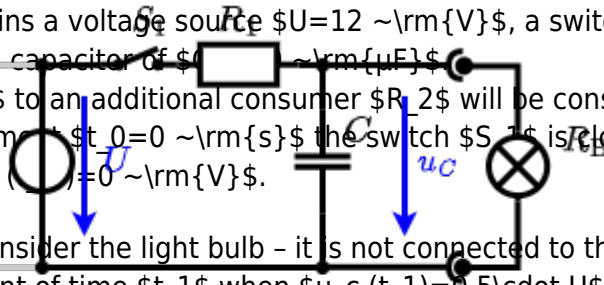
Solution
 To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

The equivalent voltage source is $U_{eq} = U \cdot \frac{R_2}{R_1 + R_2}$ and the internal resistance is $R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

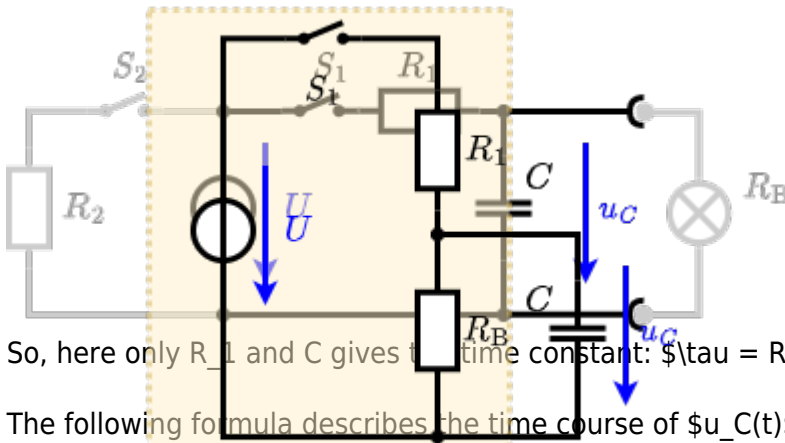


The circuit contains a voltage source $U=12 \text{ V}$, a switch S_1 , a resistor of $R_1=20 \text{ }\Omega$ and a capacitor of $C=100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0 \text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$
 An equivalent linear voltage source can be given with U_s , R_1 and R_B as seen in yellow:

$$t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

Exercise E9 Impedances at different Frequencies
 (written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC circuit has the resistor values $R_1=1 \text{ k}\Omega$ and $R_2=10 \text{ }\Omega$, and a capacitor of $C=1 \text{ }\mu\text{F}$.
 Result: $Z_B = 20 - j450 \text{ }\Omega$ ($\approx 450 \text{ }\Omega$), $Z_A = 50 - j30 \text{ }\Omega$ ($\approx 58 \text{ }\Omega$)
 A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1=40 \text{ nF}$ at $f_1=4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ }\Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on every component.

$$\underline{I}_{3R} = \underline{I}_{3R} \cdot \underline{R}_3 = \underline{I}_{3R} \cdot R_3 = \underline{I}_{3R} \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3C} = \underline{I}_{3C} \cdot \underline{X}_{3C} = \underline{I}_{3C} \cdot (-j) \cdot 30 \text{ } \Omega = -j \cdot 30 \cdot \underline{I}_{3C}$$

So it gets clear that perpendicular branches can be simplified to $\underline{I}_{3R} = \underline{I}_{3C} \cdot (-j) \cdot 30 \text{ } \Omega$ and $\underline{I}_{3C} = \underline{I}_{3R} \cdot (-j) \cdot 30 \text{ } \Omega$

Therefore the resulting current of the parallel circuit is given as:

$$\underline{I}_{3R} = \underline{I}_{3C} \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3C} = \underline{I}_{3R} \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3R} = \underline{I}_{3R} \cdot (-j) \cdot 30 \text{ } \Omega \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3R} = \underline{I}_{3R} \cdot 900 \text{ } \Omega^2$$

$$\underline{I}_{3R} = \frac{\underline{I}_{3C}}{900 \text{ } \Omega^2}$$

This can be rearranged to get $\underline{I}_{3R} = \frac{\underline{I}_{3C}}{900 \text{ } \Omega^2}$

Back to the first formula:

$$\underline{I}_{3R} = \underline{I}_{3C} \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3C} = \frac{\underline{I}_{3R}}{-j \cdot 30 \text{ } \Omega}$$

$$\underline{I}_{3R} = \frac{\underline{I}_{3R}}{-j \cdot 30 \text{ } \Omega} \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3R} = \underline{I}_{3R} \cdot (-j) \cdot 30 \text{ } \Omega \cdot (-j) \cdot 30 \text{ } \Omega$$

$$\underline{I}_{3R} = \underline{I}_{3R} \cdot 900 \text{ } \Omega^2$$

$$\underline{I}_{3R} = \frac{\underline{I}_{3C}}{900 \text{ } \Omega^2}$$

Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle of the circuit (Figure 1) if $\omega = 300 \text{ rad/s}$. Both R and X_L are in Ω . The result should be given in degrees.

After analysis, the full bridge circuit should be simplified to a single loop circuit in phase. Calculate the phase angle of the circuit.

Solution

.. Calculate the physical values of the components.

$$\underline{Z}_R = R = 10 \text{ } \Omega$$

$$\underline{Z}_L = j\omega L = j \cdot 300 \cdot 0.02 = j6 \text{ } \Omega$$

$$\underline{Z}_C = \frac{1}{j\omega C} = \frac{1}{j \cdot 300 \cdot 0.001} = -j3.33 \text{ } \Omega$$

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{10 \text{ } \Omega + j6 \text{ } \Omega - j3.33 \text{ } \Omega} = \frac{50 \text{ V}}{10 \text{ } \Omega + j2.67 \text{ } \Omega}$$

The current and voltage are in phase since the circuit is purely resistive.

Therefore, the component $6 \text{ } \Omega$ is in phase with the $10 \text{ } \Omega$ resistor.

$$\underline{I} = \frac{50 \text{ V}}{10 \text{ } \Omega + j2.67 \text{ } \Omega} = \frac{50 \text{ V}}{10.34 \text{ } \Omega \angle 14.5^\circ} = 4.83 \text{ A} \angle -14.5^\circ$$

$$\underline{I} = 4.83 \text{ A} \angle -14.5^\circ$$

The phase angle φ can be calculated as:

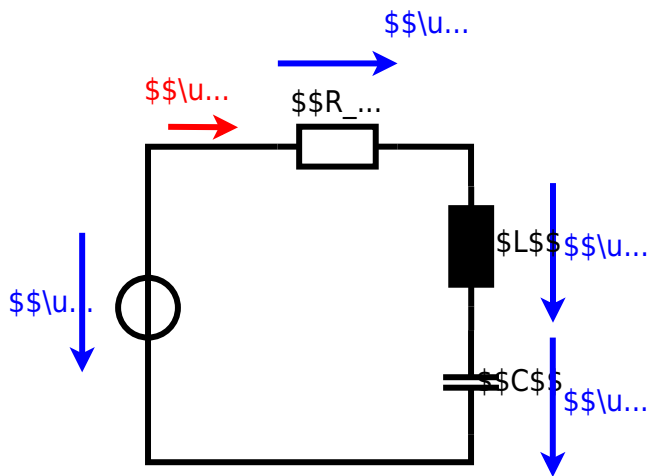
$$\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-0.75 \text{ A}}{4.68 \text{ A}}\right) = -9.1^\circ$$

With the complex part comes the complex value $\underline{I} = 4.83 \text{ A} \angle -9.1^\circ$

$$\underline{I} = 4.83 \text{ A} \angle -9.1^\circ$$

The phase angle φ can be calculated as:

$$\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-0.75 \text{ A}}{4.68 \text{ A}}\right) = -9.1^\circ$$



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