

task_kyt15w11e3sempb2_with_calculation

Student Group

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resistivity, power, exam ee1 SS2023

**Exercise E1 Equivalent linear Source
(written test, approx. 7 % of a 60-minute written test, SS2023)**

The conductivity of a dielectric material is given by $\rho(T) = \rho_0 \exp(\alpha T + \beta T^2)$ where $\rho_0 = 10^{17} \Omega^{-1} \text{m}^{-1}$ at $T = 20^\circ\text{C}$. The material is used as a dielectric in a capacitor with two parallel plates of area $A = 100 \text{ cm}^2$ and thickness $d = 1 \text{ mm}$. The plates are connected to a DC voltage source of $V = 100 \text{ V}$. Calculate the resistance of the capacitor at $T = 20^\circ\text{C}$ and $T = 55^\circ\text{C}$.

Solution
 The resistivity of the dielectric material is $\rho(T) = 10^{17} \exp(\alpha T + \beta T^2) \Omega \cdot \text{m}$.
 For the given material the temperature coefficients in the range of 20°C and 55°C are given as $\alpha = -0.048 \text{ 1/K}$ and $\beta = +0.00057 \text{ 1/K}^2$.

$$R(T) = \frac{d}{\rho(T) A} = \frac{10^{-3} \text{ m}}{10^{-4} \text{ m}^2 \cdot 10^{17} \Omega \cdot \text{m} \cdot \exp(\alpha T + \beta T^2)} = 10^{-6} \exp(-\alpha T - \beta T^2) \Omega$$

$$R(55^\circ\text{C}) = R(20^\circ\text{C}) \cdot (1 + \alpha \Delta T + \beta \Delta T^2 + \dots)$$

$$R(55^\circ\text{C}) = 80 \text{ G}\Omega \cdot (1 - 0.048 \text{ 1/K} \cdot (35 \text{ K}) + 0.00057 \text{ 1/K}^2 \cdot (35 \text{ K})^2)$$

Calculate the resistance for the dielectric material for 20°C .

Solution

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\begin{align*} R(20 \sim \text{r m } ^\circ\text{C}) \&= \rho \cdot \left\{ \frac{d}{A} \right\} \&= 10^{\{17\}} \sim \Omega \\ \text{r m m} \cdot \left\{ \left\{ 0.8 \cdot 10^{\{-6\}} \sim \text{r m m} \right\} \over \left\{ 1 \sim \text{r m m}^2 \right\} \right\} \end{align*}
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