

task_5u1zbroaz75w39jk_with_calculation

Student Group

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electrostatic, field lines, exam ee2 SS2024

Exercise E1 Electrostatics I

(written test, approx. 10 % of a 120-minute written test, SS2024)

2. What has been given to you? The charges are \$q_1 = 1 \text{ nC}\$, \$q_2 = 2 \text{ nC}\$, \$q_3 = 3 \text{ nC}\$, \$q_4 = 4 \text{ nC}\$. The value of the point charge \$q_0\$ is \$-1 \text{ nC}\$. Which value needs \$E_4\$ to have to get a resulting force of \$0 \text{ N}\$ on \$q_0\$?

Path: \$q_0 = -1 \text{ nC}\$

- \$q_1 = 2 \text{ nC}\$

Path: \$E_4 = 2310.97 \text{ (nN/m)}\$

- \$\vec{F}_{01} = \left(\begin{array}{c} 19.97 \\ 0 \\ 0 \end{array} \right) \text{ (nN)}\$

In the end, the single force components, we can calculate the resulting magnitude of the force \$F_{01}\$ by the Pythagorean theorem: \$F_{01} = \sqrt{F_{01,x}^2 + F_{01,y}^2 + F_{01,z}^2} = \sqrt{19.97^2} = 19.97 \text{ nN}\$

$$|\vec{F}_{01}| = \sqrt{\left(\sum_i F_{i,x}\right)^2 + \left(\sum_i F_{i,y}\right)^2 + \left(\sum_i F_{i,z}\right)^2} = \sqrt{19.97^2} = 19.97 \text{ nN}$$

Here, this force is the force from \$q_1\$ on \$q_0\$.

$$|\vec{F}_{01}| = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1 \cdot q_0|}{r_{01}^2} \Rightarrow r_{01} = \sqrt{\frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1 \cdot q_0|}{|\vec{F}_{01}|}} = \sqrt{\frac{1}{4\pi \cdot 8.854 \cdot 10^{-12}} \cdot \frac{2 \cdot 10^{-9}}{19.97 \cdot 10^{-9}}} = 0.05 \text{ m} = 5 \text{ cm}$$

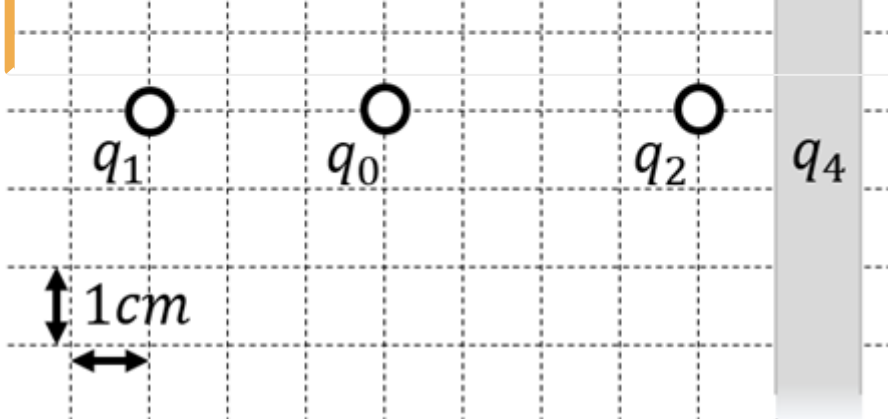
$$|\vec{F}_{01}| = |E_4| \cdot |q_0| \Rightarrow E_4 = \frac{|\vec{F}_{01}|}{|q_0|} = \frac{19.97 \cdot 10^{-9} \text{ N}}{1 \cdot 10^{-9} \text{ C}} = 19.97 \text{ N/C} = 19.97 \text{ V/m}$$

$$E_4 = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_4}{r_{04}^2} \Rightarrow r_{04} = \sqrt{\frac{1}{4\pi\epsilon_0} \cdot \frac{q_4}{E_4}} = \sqrt{\frac{1}{4\pi \cdot 8.854 \cdot 10^{-12}} \cdot \frac{4 \cdot 10^{-9}}{19.97 \cdot 10^{-9}}} = 0.1 \text{ m} = 10 \text{ cm}$$

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1. Calculate the single forces \$\vec{F}_{01}\$, \$\vec{F}_{02}\$, \$\vec{F}_{03}\$, on the charge \$q_0\$!

Path

First, calculate the magnitude of the forces, like \$\vec{F}_{01}\$.

The force \$\vec{F}_{01}\$ is purely on the \$x\$-axis and therefore equal to

$$F_{01,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1 \cdot q_0|}{r_{01}^2} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12}} \cdot \frac{2 \cdot 10^{-9}}{(0.05)^2} = 19.97 \text{ nN}$$

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$\cdot 10^{-6} \text{ \{rm \{VAs\}\over\{m\}\}} = 19.97... \cdot 10^{-6} \text{ \{rm \{Ws\}\over\{m\}\}} \quad \&= 19.97... \text{ \{rm \mu N\} \quad \text{\text{(to the right)}} \end{align*}$

Similarly, we get for \vec{F}_{02} and \vec{F}_{03} $\begin{align*} \vec{F}_{02} = F_{02,x} \quad \&= -28.09... \text{ \{rm \mu N\} \quad \text{\text{(to the right)}} \quad \\ \vec{F}_{03} \quad \&= -22.47... \text{ \{rm \mu N\} \quad \text{\text{(to the top left)}} \quad \end{align*}$

For \vec{F}_{03} , we have to calculate the x - and y -component.

This is possible, by using the angle α between the line through q_0 and q_3 and the positive x -axis (pointing to the right).

So, α has to be between 90° and 180° . It can be calculated by:

$\begin{align*} \alpha = \arctan\left(\frac{-4\text{ cm}}{+2\text{ cm}}\right) = \pi - 1.1071... = 180^\circ - 63.4...^\circ = 116.6...^\circ \end{align*}$

Based on this, the x - and y -component is: $\begin{align*} F_{03,x} \quad \&= |\vec{F}_{03}| \cdot \cos \alpha = 10.05... \text{ \{rm \mu N\} \quad \text{\text{(to the left)}} \quad \\ F_{03,y} \quad \&= |\vec{F}_{03}| \cdot \sin \alpha = 20.10... \text{ \{rm \mu N\} \quad \text{\text{(to the top)}} \quad \end{align*}$

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