

task_dtoqvpvrbdtozfk_with_calculation

Student Group

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electrostatic, field lines, exam ee2 SS2022

Exercise E1 Electrostatics I

(written test, approx. 10 % of a 120-minute written test, SS2022)

2. What has been given to you? The charges are \$q_1 = 1 \text{ nC}\$, \$q_2 = 2 \text{ nC}\$, \$q_0 = 1 \text{ nC}\$, \$q_4 = 1 \text{ nC}\$. The charges are placed on a grid with a spacing of \$1 \text{ cm}\$. The grid is shown in the picture below. The value of the permittivity of free space is \$\epsilon_0 = 8.854 \cdot 10^{-12} \text{ As/Vm}\$. Which value needs \$E_4\$ to have to get a resulting force of \$0 \text{ N}\$ on \$q_0\$?

Path: \$q_0 = 1 \text{ nC}\$

- \$q_1 = 2 \text{ nC}\$

Path: \$E_4 = 2310.97 \text{ (nN/m)}\$

- \$\vec{F}_{01} = \left(\begin{array}{c} 19.97 \\ 0 \\ 0 \end{array} \right) \text{ (nN)}\$

In the end, the single force components are calculated. The resulting magnitude of the force is \$F_{01} = 19.97 \text{ nN}\$. The force is purely on the \$x\$-axis and therefore equal to \$F_{01,x} = 19.97 \text{ nN}\$.

$$F_{01,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \text{ nC} \cdot 2 \text{ nC}}{(3 \text{ cm})^2} = 19.97 \text{ nN}$$

$$F_{02,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_2 \cdot q_0}{r_{02}^2} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{2 \text{ nC} \cdot 1 \text{ nC}}{(2 \text{ cm})^2} = 10.05 \text{ nN}$$

$$F_{03,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_3 \cdot q_0}{r_{03}^2} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \text{ nC} \cdot 1 \text{ nC}}{(1 \text{ cm})^2} = 2.26 \text{ nN}$$

$$F_{04,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_4 \cdot q_0}{r_{04}^2} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \text{ nC} \cdot 1 \text{ nC}}{(1 \text{ cm})^2} = 2.26 \text{ nN}$$

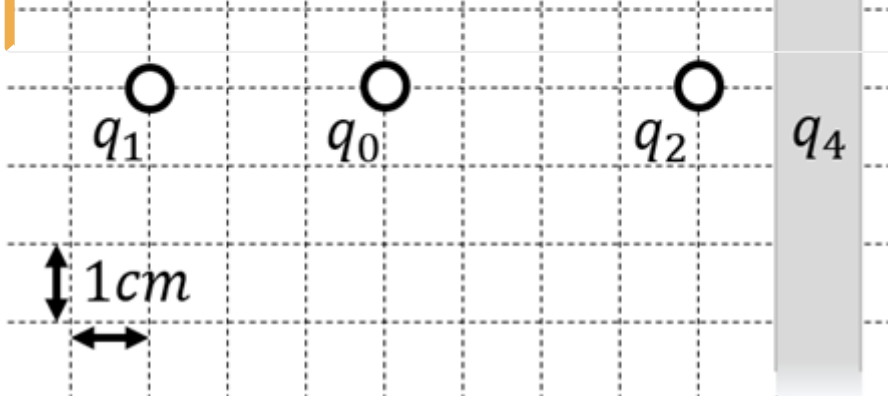
$$F_{01,x} = 19.97 \text{ nN}$$

$$F_{02,x} = 10.05 \text{ nN}$$

$$F_{03,x} = 2.26 \text{ nN}$$

$$F_{04,x} = 2.26 \text{ nN}$$

\$\vec{F}_{01} = \left(\begin{array}{c} 19.97 \\ 0 \\ 0 \end{array} \right) \text{ (nN)}\$



1. Calculate the single forces \$\vec{F}_{01}\$, \$\vec{F}_{02}\$, \$\vec{F}_{03}\$, on the charge \$q_0\$!

Path

First, calculate the magnitude of the forces, like \$\vec{F}_{01}\$.

The force \$\vec{F}_{01}\$ is purely on the \$x\$-axis and therefore equal to \$F_{01,x}\$.

$$\vec{F}_{01} = F_{01,x} \hat{x}$$

$$F_{01,x} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2}$$

$$F_{01,x} = \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \text{ nC} \cdot 2 \text{ nC}}{(3 \text{ cm})^2}$$

$$F_{01,x} = 19.97 \text{ nN}$$

$$F_{01,x} = 19.97 \text{ nN}$$

$\cdot 10^{-6} \left\{ \frac{VAs}{m} \right\} = 19.97... \cdot 10^{-6} \left\{ \frac{Ws}{m} \right\} \quad \&= 19.97... \left\{ \frac{\mu N}{\mu N} \right\} \quad \text{\texttt{(to the right)}} \end{align*}$

Similarly, we get for \vec{F}_{02} and \vec{F}_{03}

$$\vec{F}_{02} = F_{02,x} \quad \&= -28.09... \left\{ \frac{\mu N}{\mu N} \right\} \quad \text{\texttt{(to the right)}} \quad \&= -22.47... \left\{ \frac{\mu N}{\mu N} \right\} \quad \text{\texttt{(to the top left)}} \end{align*}$$

For \vec{F}_{03} , we have to calculate the x - and y -component.

This is possible, by using the angle α between the line through q_0 and q_3 and the positive x -axis (pointing to the right).

So, α has to be between 90° and 180° . It can be calculated by:

$$\alpha = \arctan\left(\frac{-4\text{~cm}}{+2\text{~cm}}\right) = \pi - 1.1071... = 180^\circ - 63.4...^\circ = 116.6...^\circ \end{align*}$$

Based on this, the x - and y -component is:

$$F_{03,x} \quad \&= |\vec{F}_{03}| \cdot \cos \alpha = 10.05... \left\{ \frac{\mu N}{\mu N} \right\} \quad \text{\texttt{(to the left)}} \quad \&= |\vec{F}_{03}| \cdot \sin \alpha = 20.10... \left\{ \frac{\mu N}{\mu N} \right\} \quad \text{\texttt{(to the top)}} \end{align*}$$

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Last update: **2024/07/04 23:41**

