

# task\_nyniewamxfshpuwt\_with\_calculation

## Student Group

First Name	Surname	Matrikel Nr.

## Table of Contents

Exercise E1 Resonant Circuit (written test, approx. 4 % of a 120-minute written test, SS2021)	2
---	---

resonance, resonant circuit, RMS, exam ee2 SS2021

**Exercise E1 Resonant Circuit**  
**(written test, approx. 4 % of a 120-minute written test, SS2021)**

6) An AC voltage source  $U_{\text{rms}} = 12 \text{ V}$  is connected in series with a resistor  $R_i = 200 \text{ m}\Omega$  and a parallel combination of a resistor  $R$  and a capacitor  $C = 30 \text{ nF}$ . The voltage across the capacitor is  $U_C = 205.4681 \text{ V}$ . The resistance  $R$  can be varied.

- $U_{\text{rms}} = 12 \text{ V}$
- $R_i = 200 \text{ m}\Omega$
- $C = 30 \text{ nF}$

For the following calculation, the internal resistance  $R_i$  and the resistance  $R$  have to be combined:

$$R_{\Sigma} = R_i + R$$

Here, either one knows that the gain factor  $Q$  stands for  $Q = \frac{U_C}{U_{\text{rms}}}$  and therefore can directly use the following formula:

$$Q = \frac{U_C}{U_{\text{rms}}} = \frac{1}{R_{\Sigma}} \sqrt{\frac{L}{C}}$$

$$R_{\Sigma} = \frac{U_{\text{rms}}}{U_C} \sqrt{\frac{L}{C}}$$

When the gain factor is not known, one has to derive it:

The voltage  $I$  at resonance is only given by the total ohmic resistance  $R_{\Sigma}$  and the source voltage  $U_{\text{rms}}$ :

$$I = \frac{U_{\text{rms}}}{R_{\Sigma}}$$

This current flow also through the impedance of the capacitor

$$U_C = Z_C \cdot I = \frac{1}{\omega C} \cdot I = \frac{U_{\text{rms}}}{\omega C R_{\Sigma}}$$

At resonance, the angular frequency  $\omega$  is given by  $\omega = \frac{1}{\sqrt{LC}}$

$$U_C = \frac{U_{\text{rms}}}{\frac{1}{\sqrt{LC}} R_{\Sigma}} = \frac{U_{\text{rms}} \sqrt{LC}}{R_{\Sigma}}$$

$$R_{\Sigma} = \frac{U_{\text{rms}} \sqrt{LC}}{U_C}$$

a) What is the resonance frequency  $f_0$ ?

Path

In both cases, we end up with the same formula, where we have to insert the physical values:

$$R_{\Sigma} = \frac{U_{\text{rms}} \sqrt{LC}}{U_C} = \frac{12 \text{ V} \cdot \sqrt{20 \cdot 10^{-3} \text{ H} \cdot 30 \cdot 10^{-6} \text{ F}}}{205.4681 \text{ V}}$$

The resonant frequency  $f_0$  is given as:

$$f_0 = \frac{1}{2\pi \sqrt{LC}} = \frac{1}{2\pi \sqrt{20 \cdot 10^{-3} \text{ H} \cdot 30 \cdot 10^{-6} \text{ F}}} = 6.2549 \text{ kHz}$$

And so, the resistance  $R$  is:

$$R = R_{\Sigma} - R_i = 6.2549 \text{ kHz} - 200 \text{ m}\Omega = 205.4681 \text{ Hz}$$

With the values  $f_0 = 6.2549 \text{ kHz}$  and  $R = 205.4681 \text{ Hz}$

From:

<https://wiki.mexle.org/> - **MEXLE Wiki**

Permanent link:

[https://wiki.mexle.org/ee2/task\\_nyniewamxfshpuwt\\_with\\_calculation](https://wiki.mexle.org/ee2/task_nyniewamxfshpuwt_with_calculation)

Last update: **2024/07/04 03:52**

