

# task\_wjttvmydrskzhcim\_with\_calculation

## Student Group

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complex voltage divider, RMS, inductor, exam ee2 SS2021

**Exercise E9 Component Parameters**  
**(written test, approx. 10 % of a 120-minute written test, SS2021)**

Determine the component parameters of a motor (motor presents a resistive inductive load) for the next exercises consider the following:  
 The RMS values of the series resistance  $R_{\text{M}}$  and the inductance  $L_{\text{M}}$  are to be determined below. Both results in the impedance of the motor.  
 For two different frequencies, the rms values of the applied voltage  $U_1$  and  $U_2$  was applied.

This resulted in the recorded current of  $I_1$  and  $I_2$ .  
 Derive in general the equation for the absolute value of the impedance of the motor.

$$Z = \sqrt{(2\pi \cdot f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

- $R_{\text{M}} = 10 \cdot \Omega$
- $L_{\text{M}} = 10 \cdot \text{mH}$

Since we have the absolute values of the impedances from the specified formulas from a) and b) this has the advantage that  $R_{\text{M}}$  will cancel out:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left( (2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

The complex impedance  $\underline{Z}$  for a resistive inductive load  $R_{\text{M}}$  and  $L_{\text{M}}$  in series circuit is given as  $\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$

Now we can rearrange to  $L_{\text{M}}$ :

The Pythagorean theorem can derive the absolute value:

$$\begin{aligned} Z_2^2 - Z_1^2 &= (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left( (2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right) \\ Z_2^2 - Z_1^2 &= (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2 \\ Z_2^2 - Z_1^2 &= (2\pi \cdot L_{\text{M}})^2 \cdot (f_2^2 - f_1^2) \\ L_{\text{M}} &= \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}} \end{aligned}$$

And then to  $L_{\text{M}}$ :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \cdot \Omega)^2 - (6.25 \cdot \Omega)^2}{(100 \cdot \text{s}^{-1})^2 - (50 \cdot \text{s}^{-1})^2}} = 14.346 \cdot \text{mH}$$

The resistance value  $R_{\text{M}}$  can be derived from  $Z_2^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2$

$$R_{\text{M}} = \sqrt{Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2}$$

The values have to be inserted also for  $R_{\text{M}}$ :

$$R_{\text{M}} = \sqrt{(10 \cdot \Omega)^2 - (2\pi \cdot 100 \cdot \text{s}^{-1} \cdot 0.014346 \cdot \text{H})^2} = 4.3301 \cdot \Omega$$

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