

# task\_6tqttque1e2nf2c7\_with\_calculation

## Student Group

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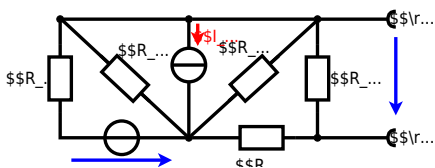
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dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 WS2022

### Exercise 1.1 : Equivalent Linear Source

(written test, approx. 14% of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.



Calculated the internal resistance  $R_i$  and the source voltage  $U_s$  of an equivalent linear voltage source on the connectors  $A$  and  $B$ .  $\begin{align*} R_1=5.0 \Omega, \&\& U_2=6.0 \text{ V}, \&\& R_3=10 \Omega, \&\& I_4=4.2 \text{ A}, \&\& R_5=10 \Omega, \&\& R_6=7.5 \Omega, \&\& R_7=15 \Omega \end{align*}$  Use equivalent sources in order to simplify the circuit!

Solution

Best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ : 
$$R_{135} = R_1 || R_3 || R_5$$
 
$$I_{24} = I_2 - I_4 = \left\{ \frac{U_2}{R_1} \right\} - I_4$$
 The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following: 
$$U_{24} = R_{135} \cdot I_{24} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit there is a voltage divider given by  $R_{135}$ ,  $R_6$  and  $R_7$ .

Therefore the voltage between  $A$  and  $B$  is given as: 
$$U_{AB} = U_{24} \cdot \left\{ \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right\} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot \left\{ \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \right\}$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0 \Omega$ , so a short-circuit): 
$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$ :

$$U_{AB} = \left\{ \frac{6.0 \text{ V}}{5.0 \Omega} \right\} - 4.2 \Omega \cdot \left\{ \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \right\} || R_{AB}$$
 
$$= 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

### Final result

$$U_{AB} = 4.5 \text{ V} \quad R_{AB} = 6 \Omega$$

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