

Exam Winter Semester 2022

Student Group

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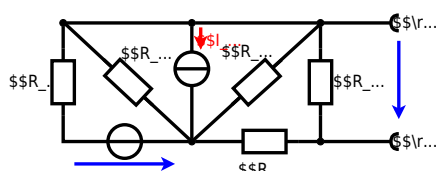
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**Exercise E1 Equivalent linear Source
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.
Result

$$U_{\text{rs}} = U_{\text{AB}} = 4.5 \text{ V}$$

$$R_{\text{i}} = R_{\text{AB}} = 6 \text{ } \Omega$$



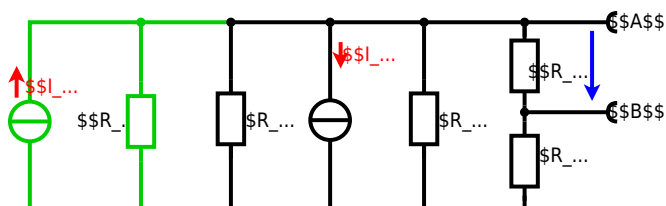
Calculated the internal resistance R_{i} and the source voltage U_{rs} of an equivalent linear voltage source on the connectors A and B .
 $R_1=5.0 \text{ } \Omega$, $U_2=6.0 \text{ V}$, $R_3= 10 \text{ } \Omega$, $I_4=4.2 \text{ A}$, $R_5=10 \text{ } \Omega$, $R_6=7.5 \text{ } \Omega$, $R_7=15 \text{ } \Omega$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot (R_6 || R_7)$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} - I_4 \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$:

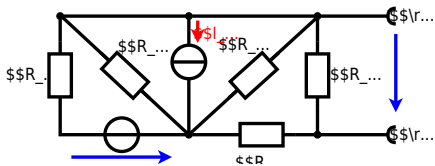
$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega}$$

$$R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

Exercise E3 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

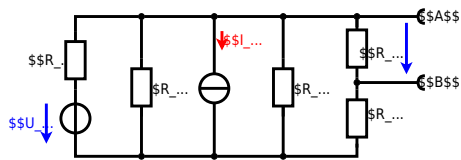
$$U_s = U_{AB} = 4.5\text{V} \quad R_i = R_{AB} = 6\Omega$$



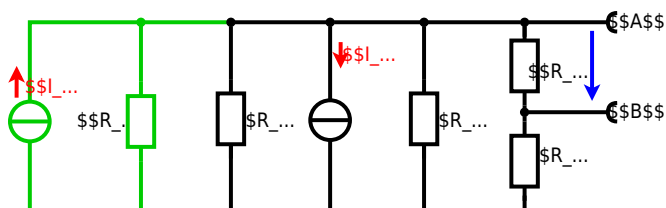
Calculate the internal resistance R_{int} and the source voltage U_s of an equivalent linear voltage source on the connectors A and B . $R_1=5.0 \Omega$, $U_s=6.0 \text{ V}$, $R_2=10 \Omega$, $I_4=4.2 \text{ A}$, $R_3=10 \Omega$, $R_4=7.5 \Omega$, $R_5=15 \Omega$ and $R_6=10 \Omega$. Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot (R_5 + R_6 || R_7)$$

$$U_{AB} = R_{135} \cdot I_{24} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \parallel R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phasor voltage \underline{U} (in V) at the terminals A and B in the circuit shown in the figure. The components (R and X_{L1}) shall be given.

After analysis, the full dimensional circuit impedance Z can be extracted and \underline{U} can be calculated. $Z = \frac{1}{\frac{1}{R} + \frac{1}{j\omega L_1}} = \frac{R \cdot j\omega L_1}{R + j\omega L_1} = \frac{10 \cdot j30}{10 + j30} = \frac{10j30}{10 + j30} = \frac{300j}{10 + j30} = \frac{300j(10 - j30)}{10^2 + 30^2} = \frac{300j(10 - j30)}{100 + 900} = \frac{300j(10 - j30)}{1000} = \frac{3000j - 9000}{1000} = -9 + j3 \Omega$

.. Calculate the physical values of the two components.

Solution: $R = 10 \Omega$ and $L_1 = \frac{30}{300} \text{ H} = 0.1 \text{ H}$

Solution: $\underline{U} = \frac{\underline{U}_0}{Z} = \frac{50 \text{ V}}{-9 + j3 \Omega} = \frac{50}{\sqrt{81 + 9}} \angle -\arctan\left(\frac{3}{-9}\right) = \frac{50}{\sqrt{90}} \angle -18.4^\circ = \frac{50}{9.487} \angle -18.4^\circ = 5.27 \angle -18.4^\circ \text{ V}$

The current and voltage are in phase and the voltage is 5.27 V (real) resulting in a power of $P = \frac{U^2}{R} = \frac{5.27^2}{10} = 0.278 \text{ W}$

Therefore, the component 4.68 mH is a capacitor with the same absolute value of 4.68 mH impedance. $X_L = j\omega L = j300 \cdot L = 4.68 \text{ mH} \Rightarrow L = \frac{4.68 \text{ mH}}{300} = 15.6 \mu\text{H}$

The absolute value of \underline{U} is 5.27 V and the phase is -18.4° . $\underline{U} = 5.27 \angle -18.4^\circ \text{ V}$

With the complex part comes the physical values $\underline{U} = 5.27 \angle -18.4^\circ \text{ V}$

The phase φ can be calculated as
$$\varphi = \arctan \left(\frac{\text{Im}(Z)}{\text{Re}(Z)} \right) = \arctan \left(\frac{-4.68 \omega}{0.24 \omega} \right)$$

Exercise E5 Analyzing complex Impedances
(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle φ of the total impedance Z in the circuit shown in the figure. The components R and X_L shall be given.

After analysis, the full width of the band is 20 MHz . The center frequency is $f_c = 300 \text{ MHz}$. The phase angle φ is 90° .
 Solution
$$Z = R + j\omega L = 10 \text{ } \Omega + j(2\pi \cdot 300 \cdot 10^6 \cdot 10^{-9}) \text{ } \Omega = 10 \text{ } \Omega + j628.3 \text{ } \Omega$$

3. Calculate the physical values of the two components.

Solution
$$\varphi = \arctan \left(\frac{\omega L}{R} \right) = 90^\circ \Rightarrow \omega L = R = 10 \text{ } \Omega$$

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{10 \text{ } \Omega + j628.3 \text{ } \Omega} = 0.0157 \text{ A} \angle -89.4^\circ$$

 The current I and voltage U are in phase since $\varphi = 0^\circ$.
 The magnitude of the current is $I = 0.0157 \text{ A}$.
 The magnitude of the voltage is $U = 50 \text{ V}$.
 The phase angle φ is 90° .
 The physical values of the two components are $R = 10 \text{ } \Omega$ and $L = 1.59 \text{ } \mu\text{H}$.

Exercise E6 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A circuit with a resistor R and a capacitor C is shown in the figure. The resistor R and capacitor C shall have the same absolute value of the impedance at $f_1 = 100 \text{ kHz}$ and $f_2 = 1 \text{ MHz}$.
 Result $R = 100 \text{ } \Omega$, $C = 1.59 \text{ nF}$.
 The resistor R shall have the same absolute value of the impedance as a capacitor C at $f_1 = 100 \text{ kHz}$ and $f_2 = 1 \text{ MHz}$.

Solution

Solution

$$\underline{R}_1 \dot{I} = \underline{R}_2 + \underline{X}_{L2} \dot{I}$$
 Since $\dot{I} \cdot \omega L$ is perpendicular to \underline{U} , this can be simplified to:

$$\underline{X}_{L2} \dot{I} \cdot \underline{I} = \underline{R}_2 \dot{I} \cdot \underline{I}$$
 So it gets clear that \underline{I}_{3R} is perpendicular to \underline{I}_{3C} (It has to, since \underline{R}_3 is perpendicular to $\dot{I} \cdot X_{L3}$, too).

Therefore the resulting current of the parallel circuit is given as:

$$\underline{I}_{3R} = \sqrt{|\underline{I}_{3C}|^2 - |\underline{I}_{3R}|^2}$$

Back to the first formula:

$$\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} \cdot \frac{|\underline{I}_{3C}|}{|\underline{I}_{3R}|} = \frac{1}{2\pi \cdot f \cdot C_3} \cdot \frac{|\underline{I}_{3C}|}{|\underline{I}_{3R}|} \cdot \sqrt{|\underline{I}_{3C}|^2 - |\underline{I}_{3R}|^2}$$

Exercise E6 Impedances at different Frequencies
 (written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by:

$$\underline{Z} = R + j\omega L$$
 Parallel circuit means that the voltage is the same on R_1 and C_1 :

$$\underline{U} = \underline{R}_1 \dot{I}_1 = \underline{C}_1 \dot{I}_2$$
 Since $\dot{I}_1 \cdot \omega L$ is perpendicular to \underline{U} , this can be simplified to:

$$\underline{X}_{L2} \dot{I}_1 = \underline{R}_2 \dot{I}_1$$
 So it gets clear that \underline{I}_{3R} is perpendicular to \underline{I}_{3C} (It has to, since \underline{R}_3 is perpendicular to $\dot{I} \cdot X_{L3}$, too).

Solution

$$\underline{R}_1 = 1.00 \cdot \omega$$

$$\underline{R}_2 = 10.0 \cdot \omega$$

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by:

$$\underline{Z} = R + j\omega L$$
 Parallel circuit means that the voltage is the same on R_1 and C_1 :

$$\underline{U} = \underline{R}_1 \dot{I}_1 = \underline{C}_1 \dot{I}_2$$
 Since $\dot{I}_1 \cdot \omega L$ is perpendicular to \underline{U} , this can be simplified to:

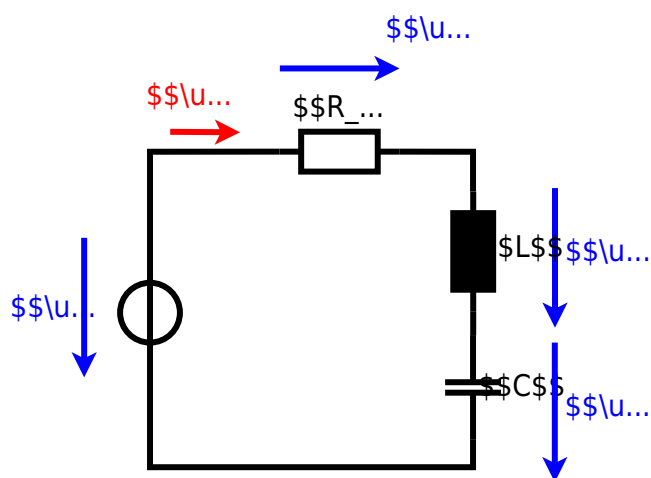
$$\underline{X}_{L2} \dot{I}_1 = \underline{R}_2 \dot{I}_1$$
 So it gets clear that \underline{I}_{3R} is perpendicular to \underline{I}_{3C} (It has to, since \underline{R}_3 is perpendicular to $\dot{I} \cdot X_{L3}$, too).

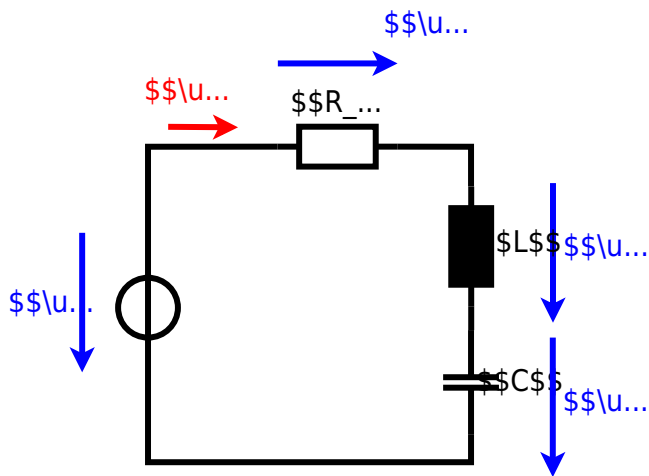
Therefore the resulting current of the parallel circuit is given as:

$$\underline{I}_{3R} = \sqrt{|\underline{I}_{3C}|^2 - |\underline{I}_{3R}|^2}$$

Back to the first formula:

$$\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} \cdot \frac{|\underline{I}_{3C}|}{|\underline{I}_{3R}|} = \frac{1}{2\pi \cdot f \cdot C_3} \cdot \frac{|\underline{I}_{3C}|}{|\underline{I}_{3R}|} \cdot \sqrt{|\underline{I}_{3C}|^2 - |\underline{I}_{3R}|^2}$$





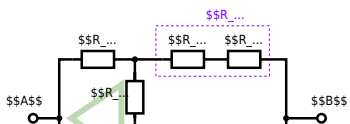
Exercise E3 Pure Resistor Network Simplification
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved at 100% of the given points. The result shall be given.

Solution

$$R_{\text{eq}} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

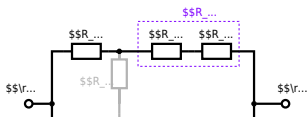
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel (R_Y + R_2) \parallel (R_Y + R_2)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between terminals A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel R_{\text{eq}} = (500 \sim \Omega) \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \frac{\{500 \sim \Omega \cdot 200 \sim \Omega\}}{500 \sim \Omega + 200 \sim \Omega}$$

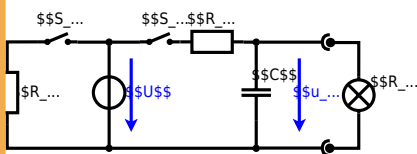
Exercise E4 Charging Capacitors
 (written test, approx. 16 % of a 60-minute written test, WS2022)

The capacitor is initially fully charged, the switch is open. The voltage across the capacitor is again U_0 at the moment $t_0 = 0$ s when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1$ ms after closing the switch.

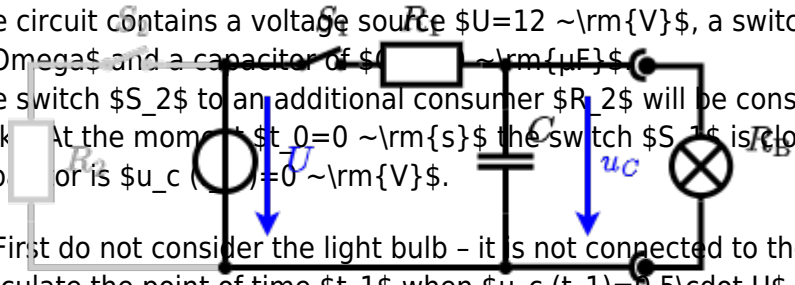
Result: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\text{eq}} = \frac{U \cdot R_2}{R_1 + R_2} \quad \text{and} \quad R_{\text{eq}} = R_1 \parallel R_2 = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

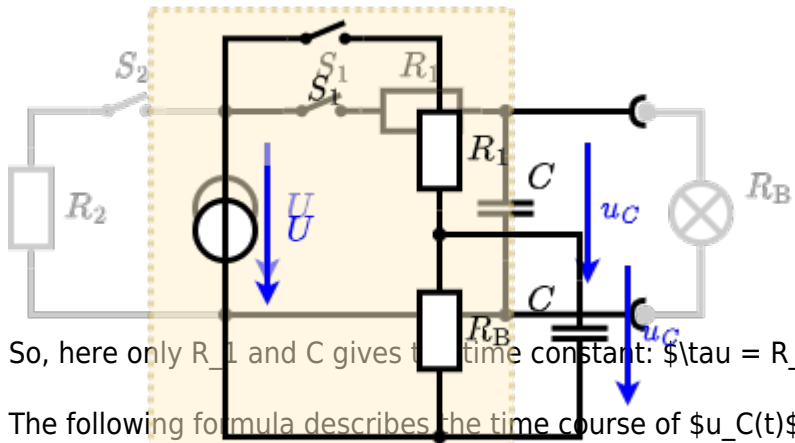


The circuit contains a voltage source $U=12 \text{ V}$, a switch S_1 , a resistor of $R_1=20 \text{ }\Omega$ and a capacitor of $C=100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0 \text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$.
 An equivalent linear voltage source can be given with U_s , R_1 and R_B as seen in yellow:

$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($=0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($=0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

Exercise E4 Charging Capacitors
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (as shown in the figure) consists of a DC voltage source $U=6 \text{ V}$, a resistor $R_1=20 \text{ }\Omega$, a capacitor $C=20 \text{ }\mu\text{F}$ and a light bulb $R_B=20 \text{ }\Omega$. The switch S_1 is open. The voltage across the capacitor is again 0 V at the moment $t_0=0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1 \text{ ms}$ after closing the switch.

Solution To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

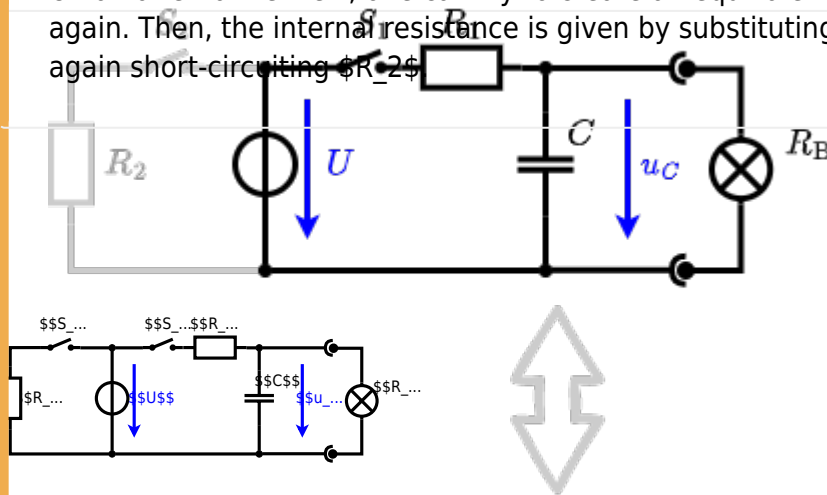
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = 3 \text{ V}$$

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

Solution

The ideal voltage source is $U = 12 \text{ V}$. The internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

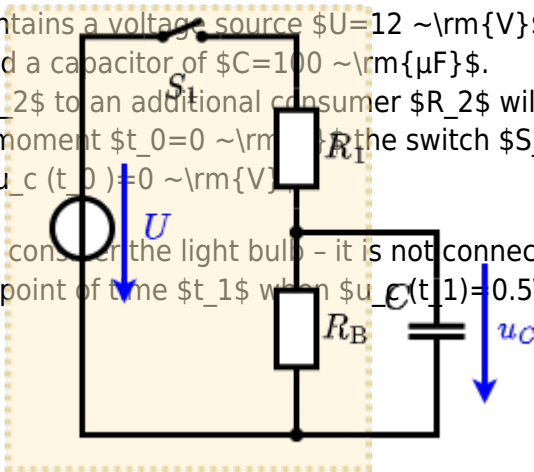
On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first asks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R = 0 \text{ }\Omega$, short-circuit). $R_i = R_1 \parallel R_B = 10 \text{ }\Omega$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$: $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$. It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

Exercise E2 Temperature-dependent Resistance
(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, explains a thermodynamic system in a refrigerator. The food has a resistance of $10 \text{ k}\Omega$ at 25°C . Your answer.

Its temperature coefficients are: $\alpha=0.01 \text{ K}^{-1}$ and $\beta=71 \cdot 10^{-6} \text{ K}^{-2}$

Result
The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The power transfer is $P = U \cdot I$ and $I = \frac{U}{R}$. Therefore, a solution is to increase the resistance of the thermistor.
Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$
$$\Delta T = T_{\text{end}} - T_{\text{start}}$$
$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

Exercise E2 Temperature-dependent Resistance
(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, explains a thermodynamic system in a refrigerator. The food has a resistance of $10 \text{ k}\Omega$ at 25°C . Your answer.

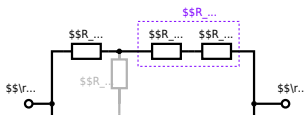
Its temperature coefficients are: $\alpha=0.01 \text{ K}^{-1}$ and $\beta=71 \cdot 10^{-6} \text{ K}^{-2}$

Result
The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The power transfer is $P = U \cdot I$ and $I = \frac{U}{R}$. Therefore, a solution is to increase the resistance of the thermistor.
Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$
$$\Delta T = T_{\text{end}} - T_{\text{start}}$$
$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim\Omega + 200 \sim\Omega + 200 \sim\Omega) \parallel (100 \sim\Omega + 100 \sim\Omega) \parallel R_{\text{eq}} = (500 \sim\Omega) \parallel (200 \sim\Omega) \parallel R_{\text{eq}} = \frac{500 \sim\Omega \cdot 200 \sim\Omega}{500 \sim\Omega + 200 \sim\Omega}$$

Exercise E1 Resistance of a Wire by Resistivity
(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The heating element is used to heat the wire with a temperature of $180 \sim\text{C}$. The electric power dissipation (= heat flow) of $P=40 \sim\text{W}$ is necessary. Determine the current I needed to operate it for heating elements. The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \sim\Omega \cdot \text{m}$.

The heating element is $3 \sim\text{m}$ long and has a diameter of $3.57 \sim\text{mm}$.
 Solution: Calculate the resistance R of the heating element.

Solution

$$P = U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \sim\text{W}}{0.33 \sim\Omega}}$$

$$R = \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad \parallel \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \parallel \quad R = 1.10 \cdot 10^{-6} \sim\Omega \cdot \text{m} \cdot \frac{4 \cdot 3 \sim\text{m}}{(3.57 \cdot 10^{-3} \sim\text{m})^2 \cdot \pi}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire with a temperature of 180°C . Electric power dissipation (= heat flow) of $P=40\text{ W}$ is necessary.

Calculate the current I needed to operate for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6}\ \Omega\text{m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{ W}}{0.33\ \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \text{and } R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ &= 1.10 \cdot 10^{-6}\ \Omega\text{m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

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