

task_yh4srwxu1bo1rdy4_with_calculation

Student Group

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resonance, impedance, resonant circuit, exam ee2 SS2024

Exercise E18 Magnetic Circuit

(written test, approx. 10 % of a 120-minute written test, SS2024)

2. For a series RLC circuit, the components are: a resistor with resistance $R = 5 \text{ } \Omega$, an inductor with inductance $L = 1.6 \text{ nH}$, and a capacitor with capacitance $C = 10 \text{ nF}$. The circuit is connected to an AC voltage source $U_C = 100 \text{ V}$ with a frequency $f_0 = 44 \text{ MHz}$. What is the resonance frequency f_r and the impedance Z_{RLC} at resonance? (Phase and magnitude)

Path

- $U_C = 100 \text{ V}$
- $f_0 = 44 \text{ MHz}$
- $R = 5 \text{ } \Omega$
- $L = 1.6 \text{ nH}$
- $C = 10 \text{ nF}$

The formula for the resonance frequency f_r is:

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

The voltage across the capacitor is:

$$U_C = U \cdot Q = U \cdot \frac{\omega L}{R}$$

The impedance at resonance is:

$$Z_{RLC} = R = 5 \text{ } \Omega$$

A given capacitor shall have the following values:

- $C = 10 \text{ nF}$
- $R = 20 \text{ m}\Omega$
- $L = 1.6 \text{ nH}$

1. What is the impedance Z_{RLC} of this real capacitor for $f_0 = 44 \text{ MHz}$? (Phase and magnitude)

Path

The impedance is based on the resistance R and the reactance $X_{LC} = j(X_L - X_C)$:

$$\underline{Z}_{RLC} = R + j(\omega L - \frac{1}{\omega C}) = R + j(2\pi f \cdot L - \frac{1}{2\pi f \cdot C})$$

The reactive part is:

$$X_{LC} = 2\pi f \cdot L - \frac{1}{2\pi f \cdot C}$$

$$C \} \ \&= \ 2\pi \ 44 \ \cdot \ 10^{\{6\}} \ \{\sim\text{MHz}\} \ \cdot \ 1.6 \ \cdot \ 10^{\{-9\}} \ \{\sim\text{H}\} - \\ \{\{1\}\over{\{2\pi \ \cdot \ 10^{\{6\}} \ \{\sim\text{MHz}\} \ \cdot \ 10 \ \cdot \ 10^{\{-9\}} \ \{\sim\text{F}\}\}} \} \ \&= \\ +0.08062... \ \sim\Omega \ \& \ \end{align*}$$

To get the magnitude of the impedance $|\underline{Z}_{RLC}|$ one can use the Pythagorean Theorem:
$$|\underline{Z}_{RLC}| \ \&= \ \sqrt{R^2 + X_{LC}^2} \ \&= \ \sqrt{(0.020 \ \sim\Omega)^2 + (0.08062... \ \sim\Omega)^2} \ \&= \ 0.0830 \dots \ \sim\Omega \ \& \ \end{align*}$$

For the phase φ the \arctan can be applied:
$$\varphi \ \&= \ \arctan \left(\frac{X_{LC}}{R} \right) \ \&= \ \arctan \left(\frac{0.08062... \ \sim\Omega}{0.020 \ \sim\Omega} \right) \ \&= \ 1.3276 \dots \ \hat{=} \ +76^\circ \ \& \ \end{align*}$$

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