

# Block 17 — Magnetic Flux Density and Forces

## Student Group

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# Block 17 — Magnetic Flux Density and Forces

## Learning objectives

After this 90-minute block, you can

- ...

## Preparation at Home

Well, again

- read through the present chapter and write down anything you did not understand.
- Also here, there are some clips for more clarification under 'Embedded resources' (check the text above/below, sometimes only part of the clip is interesting).

For checking your understanding please do the following exercises:

- ...

## 90-minute plan

1. Warm-up (x min):
  1. ....
2. Core concepts & derivations (x min):
  1. ...
3. Practice (x min): ...
4. Wrap-up (x min): Summary box; common pitfalls checklist.

## Conceptual overview

1. ...

## Core content

...

## Common pitfalls

- ...

# Exercises

## Exercise E7 Cylindrical Coil

(written test, approx. 6 % of a 120-minute written test, SS2021)

A) The magnetic flux (2 points) information is given:

Result

- Length  $l = 30 \text{ cm}$ ,

Path Winding diameter  $d = 390 \text{ mm}$ ,

- Number of windings  $N = 240$ ,
- Current in the conductor  $I = 500 \text{ mA}$ ,

• Material inside: Air

•  $\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/Am}$

The magnetic field strength is  $B = \mu_0 \mu_r H$ :

The proportion of the magnetic voltage outside the coil can be neglected. Determine the following for the inside of the coil:

$\Phi = B \cdot A$

a) Determine the magnetic field strength  $H$  and the magnetic flux  $\Phi$ .

$A = \pi r^2 = \pi \left(\frac{d}{2}\right)^2$

Path

Therefore:  $\Phi = B \cdot \pi \left(\frac{d}{2}\right)^2$

Putting in the numbers:  $\Phi = 0.0005026... \text{ Vs/m}^2 \cdot \pi \left(\frac{0.39 \text{ m}}{2}\right)^2 = 0.00006004 \text{ Vs}$

Putting in the numbers:  $H = \frac{240 \cdot 0.5 \text{ A}}{0.3 \text{ m}}$

## Exercise E3 Magnetic Flux Density

(written test, approx. 6 % of a 120-minute written test, SS2021)

A) The circuit for the experiment is shown in the laboratory. A series circuit with an

Result:  $I = 100 \text{ A}$  is operated.

Two standard coils and their  $\mu_r$  values are given. (3 points, independent)

The figure below shows the top view of the laboratory with the supply line between  $A$  and  $B$ .

Path:  $B = 0.2 \text{ m}$

$\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/Am}$ ,  $\mu_r = 1$

The formula for the magnetic field strength can be rearranged:  $H =$

$$\frac{I}{2\pi \cdot r} \quad r \quad = \quad \frac{I}{2\pi \cdot H} \quad \end{align*}$$

Again, the magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Therefore: 
$$r \quad = \quad \mu_0 \mu_r \left\{ \frac{I}{2\pi \cdot B} \right\} \quad = \quad 4\pi \cdot 10^{-7} \left\{ \frac{\text{Vs}}{\text{Am}} \right\} \left\{ \frac{100 \sim \text{A}}{2\pi \cdot 100 \cdot 10^{-6} \sim \text{T}} \right\} \quad \end{align*}$$

a) What is the highest magnetic flux density through the line in your body? (3 points)

Path

The magnetic field strength for a conducting wire is given as:

$$\begin{align*} H &= \frac{I}{2\pi \cdot r} \end{align*}$$

The magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Here, the maximum current is  $\hat{I} = 100 \sim \text{A}$  and the distance to the cable is  $r = \sqrt{(0.1 \sim \text{m})^2 + (0.4 \sim \text{m})^2} = 0.412... \sim \text{m}$ .

Therefore: 
$$B \quad = \quad 4\pi \cdot 10^{-7} \left\{ \frac{\text{Vs}}{\text{Am}} \right\} \cdot 1 \cdot \left\{ \frac{100 \sim \text{A}}{2\pi \cdot 0.412... \sim \text{m}} \right\} \quad \end{align*}$$

**Exercise E5 Toroidal Coil****(written test, approx. 5 % of a 120-minute written test, SS2021)**

A magnetic field with a flux density of at least  $50 \text{ mT}$  is to be achieved in a ring-shaped coil (toroidal coil).

The coil has 60 turns, wound around soft iron with  $\mu_r = 1200$ .

The average field line length in the coil should be  $l = 12 \text{ cm}$ .

Result:  $I_{\text{min}} = 4 \text{ A}$



What is the minimum current that must flow through a single winding?

Path

The magnetic field strength of a toroidal coil is given as:

$$\begin{aligned} H &= \frac{N \cdot I}{l} \end{aligned}$$

Based on the flux density the magnetic field strength can be derived by  $B = \mu_0 \mu_r \cdot H$ .

By this, the formula can be rearranged:

$$\begin{aligned} H &= \frac{N \cdot I}{l} \quad \parallel \quad \frac{B}{\mu_0 \mu_r} &= \\ \frac{N \cdot I}{l} &\parallel I &= \frac{B \cdot l}{\mu_0 \mu_r \cdot N} \\ \end{aligned}$$

Putting in the numbers:

$$\begin{aligned} I &= \frac{0.05 \text{ T} \cdot 0.12 \text{ m}}{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1'200 \cdot 60} \parallel &= \\ &= 0.6631... \frac{\text{T} \cdot \text{m}}{\frac{\text{Vs}}{\text{Am}}} &= 0.6631... \frac{\text{Vs}}{\text{m}^2} \cdot \text{m} \parallel &= \\ &= 0.6631... \text{ A} \end{aligned}$$

### Exercise E1 Lorentz Force (hard!)

(written test, approx. 10 % of a 120-minute written test, SS2021)

A) ~~300 picture below shows straight high voltage direct wire of the dimensions shown in the picture. A current of  $I = 200 \text{ A}$  flows through the wire.~~  
 Result: A component of  $F = 1'200 \text{ N}$  of the force acts? (Independent)

A homogeneous geomagnetic field is assumed. The magnetic field strength has a vertical component of  $B_v = 40 \mu\text{T}$  and a horizontal component of  $B_h = 20 \mu\text{T}$ .

Only a  $1'500 \text{ N}$  is perpendicular to  $\vec{B}_v$  and to  $\vec{F}_h$  and points in the right direction by the right-hand rule.

The angle between the transmission line and the horizontal component of the field strength is  $\alpha = 20^\circ$ .  
 The picture on the right shows the line (black), the field strength components, and the angle in front and top view for illustration purposes.

- a) Calculate the force that results from the current flow on the entire conductor. First, calculate the vertical and horizontal components and combine them accordingly.

Path  
Top View

**Path**

The force on the transmission line can be calculated via the Lorentz force

$$\vec{F} = I \cdot (\vec{l} \times \vec{B})$$

- The horizontal component  $F_h$  of the force is based on the vertical component  $B_v$  of the magnetic field.
- The vertical component  $F_v$  of the force is based on the horizontal component  $B_h$  of the magnetic field.

Here, we have two components for the current and therefore for the force - to evaluate.

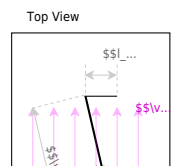
Considering the right-hand rule (and the cross product), the vertical field  $B_v$  generates a horizontal force  $F_h$  and vice versa.

The **horizontal component** is given by



$$\begin{aligned} F_{\text{h}} &= I \cdot (I \cdot B_{\text{v}}) = 1'200 \text{ A} \cdot 300 \\ &\cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} = 14'400 \\ &\frac{\text{VA}}{\text{m}} = 14'400 \frac{\text{Ws}}{\text{m}} = 14'400 \text{ N} \end{aligned}$$

For the **vertical component** the angle  $\alpha$  has to be considered.  
 For the maximum  $F_{\text{v}}$  the angle  $\alpha$  has to be  $90^\circ$ , therefore the  $\sin$  has to be used.



$$\begin{aligned} F_{\text{v}} &= I \cdot I \cdot B_{\text{h}} \cdot \sin \alpha = 1'200 \\ &\text{ A} \cdot 300 \cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} \\ &\cdot \sin 20^\circ = 2'462.545... \text{ N} \end{aligned}$$

For the **overall force**  $F$  the Pythagorean theorem has to be used:

$$\begin{aligned} F &= \sqrt{F_{\text{v}}^2 + F_{\text{h}}^2} = \sqrt{(14'400 \text{ N})^2 + (2'462.545... \text{ N})^2} \\ &= 14'609.04... \text{ N} \end{aligned}$$

## Embedded resources

Explanation (video): ...

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Permanent link:

[https://wiki.mexle.org/electrical\\_engineering\\_and\\_electronics\\_1/block17?rev=1763838980](https://wiki.mexle.org/electrical_engineering_and_electronics_1/block17?rev=1763838980)

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