Exam Summer Semester 2024

Student Group

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Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E1 Electrostatics I
(written test, approx. 8 % of a 120-minute written test, SS2024)

3. What is the magnitude of the resulting force on the charge q_0? The values of the homogenous charges E_4. Which value needs E_4 to have to get a resulting force of $0 ~\rm N$ on q_0?

- $q_0 = -1 ~\rm nC$
- $q_1 = -5 ~\rm nC$
- $E_4 = 1500 {~\rm kV}{\rm m}$
- $\vec{F}_{01} = \left({\begin{array}{cccc} +917 {~\rm \mu N} \\ 0 \\ \end{array} } \right)$
- $\vec{F}_{02} = \left({\begin{array}{cccc} -1997 {~\rm \mu N} \\ 0 \\ \end{array} } \right)$
- $\vec{F}_{03} = \left({\begin{array}{cccc} 0 ~\rm \mu N \\ -1123 {~\rm \mu N} \\ \end{array} } \right)$

With the given field components, we can calculate the resulting magnitude of the force with Pythagoras theorem $\varepsilon_0 = 8.854 \cdot 10^{-12} ~\rm As/Vm$

$$\begin{align*} |\vec{F}| &= \sqrt{\left(\sum_i F_{i,x} \right)^2 + \left(\sum_i F_{i,y} \right)^2} \\ &= \sqrt{\left(917 - 1997 + 0 \right)^2 + \left(0 + 0 - 1123 \right)^2} \\ &= 1560.\;.\!.\!.\! {~\rm \mu N} \\ \end{align*}$$

Here, this field creates a force on the force $\vec{F}_{01}$ from q_1 on q_0:

$$\begin{align*} |\vec{F}_{01}| &= |E_4| \cdot |q_0| \\ \rightarrow E_4 &= {{|\vec{F}_{01}|}\over{|q_0|}} \\ &= {{917.\;.\!.\!.\! \cdot 10^{-6} {~\rm N}}\over{1 \cdot 10^{-9} ~\rm C }} \\ &= 917.\;.\!.\!.\! \cdot 10^{3}{{\rm N}\over{\rm C}} \\ &= 917.\;.\!.\!.\! \cdot 10^{3}{{\rm VAs/m}\over{\rm As}} \\ &= 917.\;.\!.\!.\! \cdot 10^{3}{{\rm V}\over{\rm m}} \\ \end{align*}$$

1. Calculate the single forces $\vec{F}_{01}$, $\vec{F}_{02}$, $\vec{F}_{03}$, on the charge q_0!

Path

First, set up a coordinate system. Here, I choose x pointing to the right (positive values to the right) and y pointing upwards (positive values upwards).

Then, calculate the magnitude of the forces, like $\vec{F}_{01}$ (force on q_0 from q_1).
The force $\vec{F}_{01}$ is purely on the x-axis and therefore equal to $F_{01,x}$.
$$\begin{align*} \vec{F}_{01} = F_{01,x} &= {{1}\over{4\pi\varepsilon}}\cdot {{q_1\cdot q_0}\over{r^2_{01}}} \\ &= {{1}\over{4\pi\cdot 8.854 \cdot 10^{-12} ~\rm As/Vm}}\cdot {{1 \cdot 10^{-9} ~\rm C \cdot 5 \cdot 10^{-9} ~\rm C}\over{(7 \cdot 10^{-3} ~\rm m)^2}} \\ &= 917.\;.\!.\!.\! \cdot 10^{-6} {\rm {{(As)^2 \cdot Vm}\over{As \cdot m^2}}} = 917.\;.\!.\!.\! \cdot 10^{-6} {\rm {{VAs}\over{m}}} = 917.\;.\!.\!.\! \cdot 10^{-6} {\rm {{Ws}\over{m}}} \\ &= +917.\;.\!.\!.\! {\rm \mu N} \end{align*}$$
Since both q_0 and q_1 have the same sign for their charges, they are repelling each other. Therefore, The force $\vec{F}_{01}$ points to the right (positive value).

Similarly, we get for $\vec{F}_{02}$ and $\vec{F}_{03}$
$$\begin{align*} \vec{F}_{02} = F_{02,x} &= -1997.\;.\!.\!.\! {\rm \mu N} \\ \vec{F}_{03} = F_{03,y} &= -1123.\;.\!.\!.\! {\rm \mu N} \\ \end{align*}$$
Since q_0 and q_2 have the different sign for their charges, they are attract each other. Therefore, The force $\vec{F}_{02}$ points to the left (negative value).
Since q_0 and q_3 have the different sign for their charges, they are attract each other. Therefore, The force $\vec{F}_{03}$ points downwards (negative value).

Exercise E3 Electrostatics II
(written test, approx. 10 % of a 120-minute written test, SS2024)

You must analyze an aluminum profile for usage in an environment critical for electrostatic discharge.

The figure on the right shows the cross-section of the aluminum element (hatched). During the application, it might get charged up. All areas in white consist of air (= dielectric).

Six designated areas are shown by dashed frames and numbers n, which are partly inside the object.
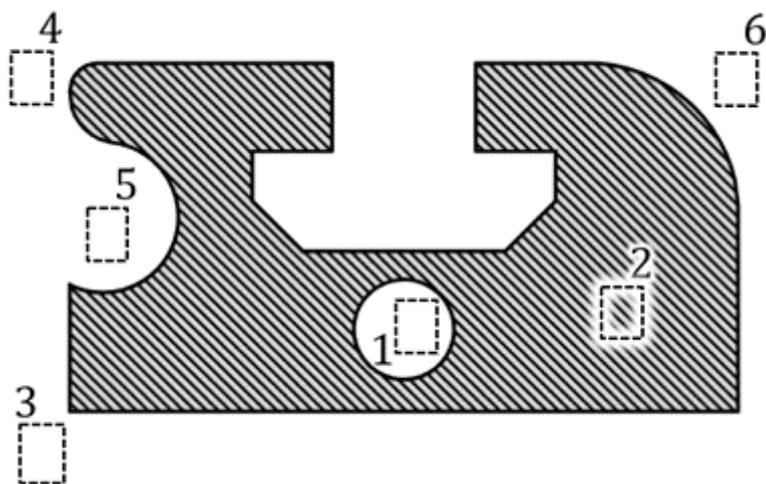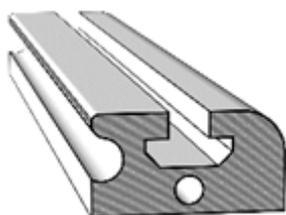
Arrange the designated areas clearly according to ascending field strengths $|\vec{E}_n|$ (absolute magnitude)! Indicate also, if designated areas have quantitatively the same field strength.

Result

$|E_1|=|E_2|=0 < |E_5| < |E_6| < |E_4| < |E_3|$

Exercise E5 Capacitor
(written test, approx. 12 % of a 120-minute written test, SS2024)

3. Calculate the capacity for a situation where a thin layer of contaminant with a thickness of $x=3 ~\rm \mu m$ is applied.

The contaminant has $\varepsilon_{\rm r,c}>\varepsilon_{\rm r,air}$, while the distance between the plates remains the same. Give a generalized formula $C_2=f(A,d,x,\varepsilon_{\rm r,c}, \varepsilon_{\rm r,air})$.

$Q = {{ \varepsilon_0 \cdot A \cdot \varepsilon_{\rm r, air} \cdot \varepsilon_{\rm r, c} }\over{ {(d-x)\cdot{\varepsilon_{\rm r,c} }} + {x\cdot{ \varepsilon_{\rm r, air}}} }}$

There are two ways now. Either: \begin{align*} Q &= C \cdot U = 1.1 ~\rm pF \cdot 3.3 ~V = 3.6522... ~pC \\ \end{align*} Or: \begin{align*} Q &= D \cdot A = 146 \cdot 10^{-9} ~{\rm C}\over{\rm m^2}) \cdot 25 \cdot 10^{-6} ~{\rm m^2} = 3.6522... ~pC \\ \end{align*}

The displacement field is given by: \begin{align*} D &= \varepsilon_0 \varepsilon_r E \\ &= \varepsilon_0 \varepsilon_r {{U}\over{d}} \\ &= 8.854 \cdot 10^{-12} ~\rm As/Vm \cdot 1 \cdot {{3.3 ~\rm V}\over{200 \cdot 10^{-6} ~\rm m} }\\ \end{align*}

The resulting capacity C is now a series circuit of $C_{\rm air}$ and $C_{\rm c}$. Therefore: \begin{align*} C = {{1}\over{ {{1}\over{C_{\rm air} }} + {{1}\over{ C_{\rm c}}} }} \end{align*}

With \begin{align*} C_{\rm air} &= \varepsilon_0 \varepsilon_{\rm r, air} {{A}\over{d-x}} &&= \varepsilon_0 A {{\varepsilon_{\rm r, air}}\over{d-x}} \\ C_{\rm c} &= \varepsilon_0 \varepsilon_{\rm r, c} {{A}\over{x}} &&= \varepsilon_0 A {{\varepsilon_{\rm r, c} }\over{x}} \\ \end{align*}

This leads to: \begin{align*} C = \varepsilon_0 A {{1}\over{ {{d-x}\over{\varepsilon_{\rm r, air} }} + {{x}\over{ \varepsilon_{\rm r, c}}} }} \end{align*}

In the following such a sensor is given with:

- Plate area: $A=25 ~\rm mm^2$
- Distance between both plates: $d=200 ~\rm \mu m$
- Air between the plates: $\varepsilon_{\rm r,air}=1$
- Supply voltage: $3.3 ~\rm V$
- Boundary effects on the end of the layers shall be ignored in the following calculations.

$\varepsilon_{0} =8.854 \cdot 10^{-12} ~\rm F/m $

1. Calculate the capacity C.

Path

\begin{align*} C &= \varepsilon_0 \varepsilon_r {{A}\over{d}} \\ &= 8.854 \cdot 10^{-12} ~\rm As/Vm \cdot 1 \cdot {{25 \cdot 10^{-6} {~\rm m} }\over{200 \cdot 10^{-6} {~\rm m} }} \end{align*}

Exercise E7 Magnetic Field Lines

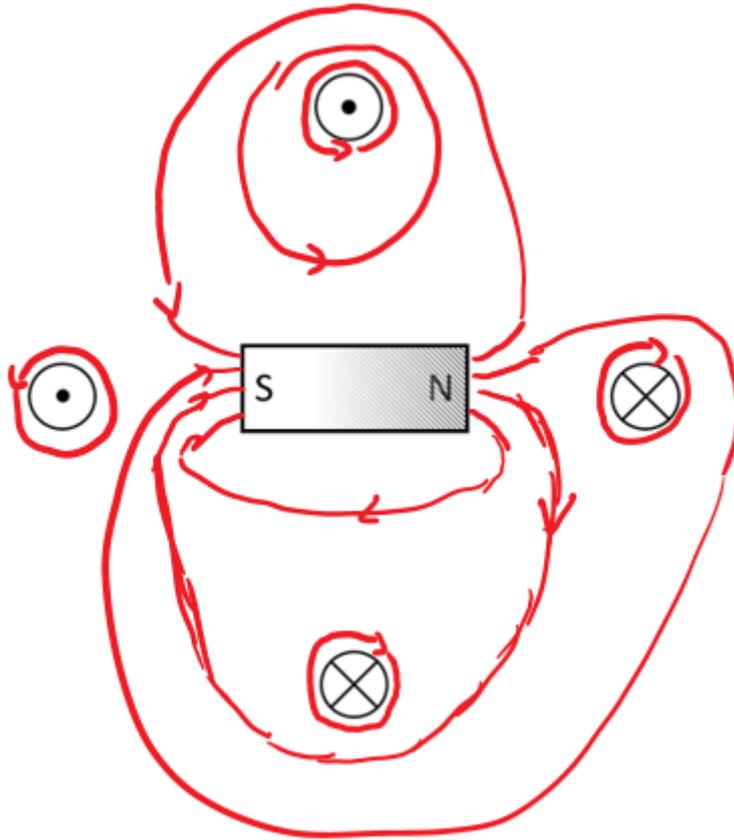**(written test, approx. 6 % of a 120-minute written test, SS2024)**

The following setup shall be given. This shows the permanent magnet affects the H-field, based on the fundamental definition of the H-field.

- Four conductors are located perpendicular to the plane of the diagram

Result: All of them conduct a current with the same magnitude, but not in the same direction.

- A permanent magnet is located in between the conductors.

- The H-field is defined by currents $\sum I = \int H {\rm d}s$.
- In the permanent magnet, there are no free currents.
- The bound currents (of the permanent magnet) create also an H field.
- This exits on the north pole and enters the magnet on the south pole (similar to the B-field)_
- $H = B/\mu$
- The H-field from task 1 gets distracted

1. D ... st 10 field lines of the H-field
qua ... and density for the shown
area

Res
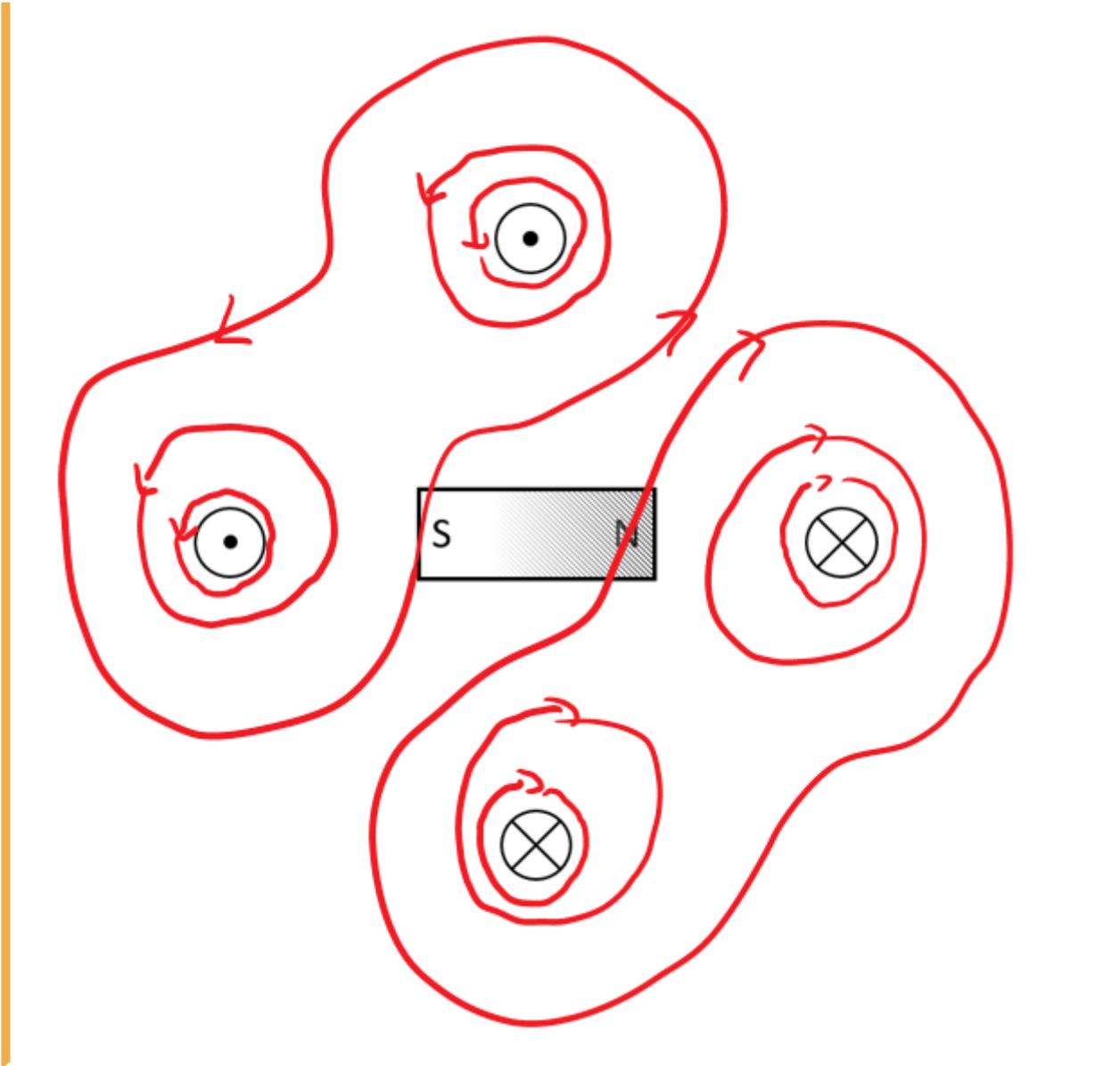
Exercise E9 Fields of an coax Cable
(written test, approx. 12 % of a 120-minute written test, SS2024)

A. Plot the graph of the magnitude of $D(x)$ with transitions [...]. The radius $+0.6 ~\rm mm$ [...] the cross-section [...] the origin in $(0|0)$ is in the center of the diagram. Use appropriate dimensions and labels for the diagram. [...] for the simulation appears:

- Inner conductor: $+3.3 ~\rm mA$, $+10 ~\rm nC$ (current into the plane of the diagram)
- Outer conductor: $-3.3 ~\rm mA$, $0 ~\rm nC$ (current out of the plane of diagram)

Results:
- for $(0.1 ~\rm mm | 0)$: $D_{\rm i} = 128...~\rm AC/m^2$
- for $(0.55 ~\rm mm | 0)$: $D_{\rm o} = 0.985...~\rm µA/m^2$

The magnitude of the electric displacement field D can be calculated by: $\int D {\rm d}A = Q$.

Here, for any position radial to the center, the surrounding area is the surface of a cylindrical shape (here for simplicity without the round endings).

This leads to:
$$\begin{align*} D(x) &= {{Q}\over{A}} \\ &= {{Q}\over{r \cdot 2\pi ...}} \end{align*}$$

- In general, the D-field is proportional to ${{1}\over{r}}$ for the situation between both conductors.
- For x within the surface of the conductor, there is no D-field such within the conductor.
- within a circle with the radius x.

\cdot x This is proportional to the area within this radius. Therefore, Ther formula $H = {{I}\over{2 \pi \cdot r}} $ gets $H(x) = {{I}\over{2 \pi \cdot x}} \cdot {{\pi ...}}$ ... and ... leads to a formula proportional to x.

So, we get for $D_{\rm i}$ ... For x within the outer conductor one also gets a linear proportionality with a similar approach.

\begin{align*} D_{\rm i} &= {{Q }\over{2 \pi \cdot r_{\rm i} \cdot l}} \\ &= {{10 \cdot 10^{-9}~C}\over{2 \pi \cdot { 0.1 \cdot 10^{-3}~\rm m} \cdot 0.5 ~\rm m}} \\ D_{\rm o} &= {{Q }\over{2 \pi \cdot r_{\rm o} \cdot l}} \\ &= {{10 \cdot 10^{-9}~C}\over{2 \pi \cdot { 0.55 \cdot 10^{-3}~\rm m}\cdot 0.5 ~\rm m}} \\ \end{align*}

Hint: For the direction, one has to consider the sign of the enclosed charge. By this, we see that the D-field is positive.
But here, again only the magnitude was questioned!

.. What is the magnitude of the magnetic field strength H at $\rm (0.1 ~mm | 0)$ and $\rm (0.55 ~mm | 0)$?

Path

The magnitude of the magnetic field strength H can be calculated by: $H = {{I}\over{2 \pi \cdot r}} $
So, we get for $H_{\rm i}$ at $\rm (0.1 ~mm | 0)$, and $H_{\rm o}$ at $\rm (0.55 ~mm | 0)$:

\begin{align*} H_{\rm i} &= {{I}\over{2 \pi \cdot r_{\rm i}}} \\ &= {{+3.3 A}\over{2 \pi \cdot { 0.1 \cdot 10^{-3}~\rm m}}} \\ H_{\rm o} &= {{I}\over{2 \pi \cdot r_{\rm o}}} \\ &= {{+3.3 A}\over{2 \pi \cdot { 0.55 \cdot 10^{-3}~\rm m}}} \\ \end{align*}

Hint: For the direction, one has to consider the right-hand rule. By this, we see that the H-field on the right side points downwards.
Therefore, the sign of the H-field is negative.
But here, only the magnitude was questioned!

Exercise E11 Lorentz Force
(written test, approx. 8 % of a 120-minute written test, SS2024)

A. Describe with your own words, what is needed to lift the mobile shuttle. Explain, does the resulting force repel the pieces into the image or out of the image (see image).

Result

Path

Since the resulting force has to be perpendicular to B-field and conductor, the force has to point to the left or the right.
For a homogeneous B field ("constant magnetic field of the shuttle"), the Lorentz forces cancel each other out.
The Lorentz force can only have a lifting effect in an inhomogeneous field.
In this case, there sum of the forces results in a repulsing force, see image.
Beside boundary effects, The field gets also inhomogeneous, by the additional field of the coils.

A si
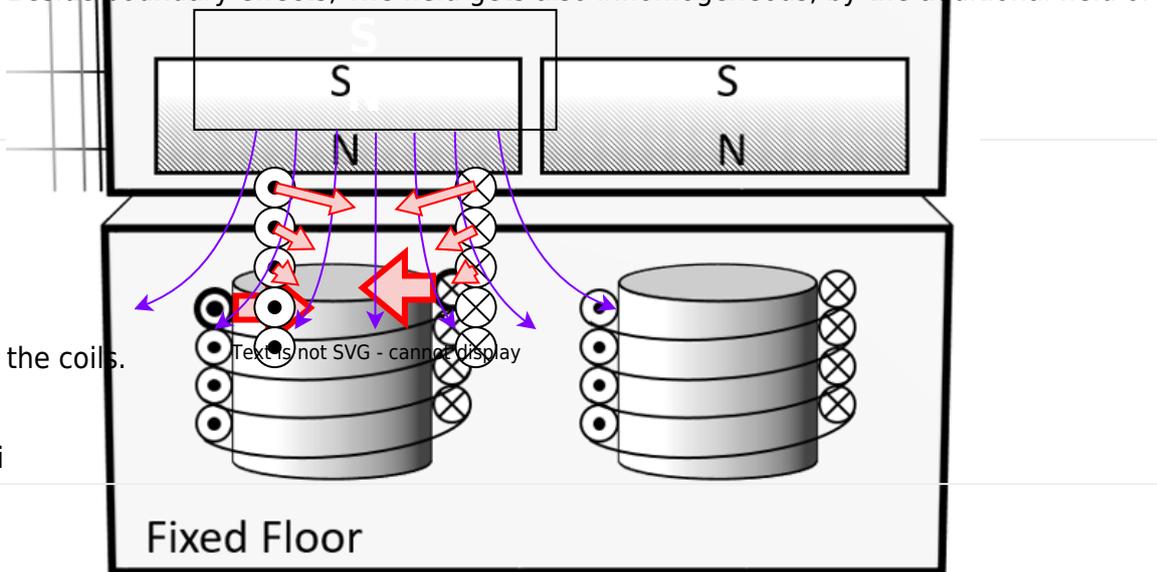
- current $I = 1.6 ~\rm A$
- magnetic field of the shuttle of is homogeneous with $B=0.5 ~\rm T$

1. Calculate the magnitude of the resulting force on one coil!

Path

The Lorentz force on a conductor the length l and the current I in a B-field is
$$\begin{align*} |\vec{F}_{L}| &= I \cdot l \cdot B \cdot \cos(\angle \vec{B}, \vec{I}) \\ &= I \cdot (N \cdot 2\pi r) \cdot B \cdot \cos(\angle \vec{B}, \vec{I}) \\ &= \rm 1.6 ~A \cdot (500 \cdot 2\pi 40\cdot 10^{-3}~m) \cdot 0.5 ~T \cdot \cos 90° \end{align*}$$

Exercise E1 Magnetic Potential
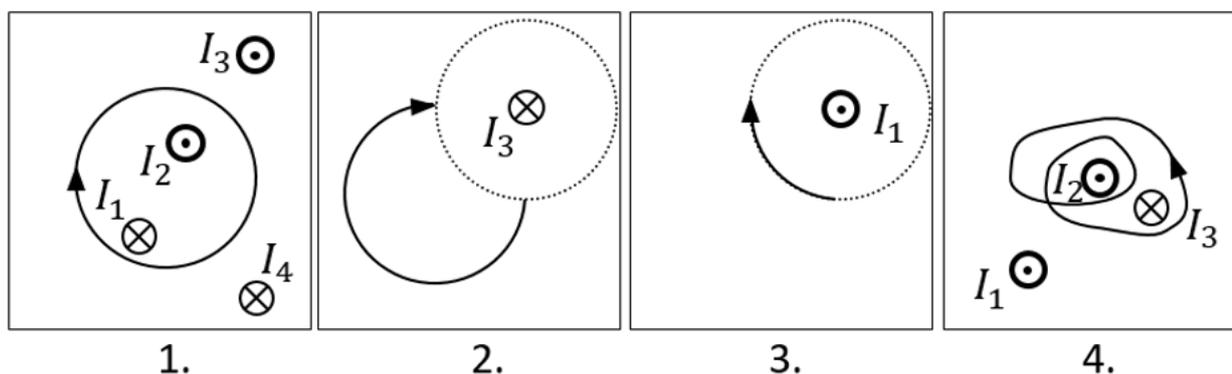## (written test, approx. 8 % of a 120-minute written test, SS2024)

Calculate the magnetic potential difference $V_\rm m$ for the following paths as shown by the solid lines.
Dotted lines are only for there for symmetry aspects!

The wires conduct the following currents:

- $|I_1|=2 ~\rm A$
- $|I_2|=5 ~\rm A$
- $|I_3|=11 ~\rm A$
- $|I_4|=7 ~\rm A$

Pay attention to the signs of the currents (given by the diagrams) and of the results!

1.   2.   3.   4.

Result

Based on the right-hand rule and the part of a full revolution the following results:

1. Task: $+I_1 - I_2 = -3 ~\rm A$

2. Task: $+{{1}\over{4}} I3 = 11/4 ~\rm A$ (it does not matter which way the path goes from the startpoint to the endpoint, as long as it has the same direction and number of revolutions)

3. Task: $-{{1}\over{4}} I1 = -0.5 ~\rm A$

4. Task: $+2 \cdot I_2 - 1 \cdot I_3 = -1 ~\rm A$

Exercise E14 Self-Induction
(written test, approx. 8 % of a 120-minute written test, SS2024)

1. Determine the inductance of a coil with a length of $30 ~\rm cm$ and a radius of $2 ~\rm cm$ and has 500 turns.

A coil with a length of $30 ~\rm cm$ and a coil radius of $2 ~\rm cm$ has 500 turns.
The current through the coil changes linearly from 0 to $3 ~\rm A$ in $0.02 ~\rm ms$.
The arrangement is located in air ($\mu_{\rm r}=1$).

Result

$\mu_0= 4\pi \cdot 10^{-7} ~\rm Vs/Am$

$u_{\rm ind}= 132 ~\rm V$

Path

2. Calculate the (self-)inductance of the coil.

For the linear change of the current the formula of the induced voltage can also be linearized: \begin{align*} u_{\rm ind} &= - L \cdot {{ {\rm d} i }\over{ {\rm d} t }} \\ &\rightarrow - L \cdot {{ {\Delta} i }\over{ {\Delta} t }} \\ &= - 1.32 \cdot 10^{-3} \cdot {{3 A}\over{0.02 \cdot 10^{-3} s}} \end{align*}

The formula for the induction of a long coil is: \begin{align*} L &= \mu_0 \mu_{\rm r} \cdot N^2 \cdot {{A}\over{l}} \\ &= 4\pi \cdot 10^{-7} {~\rm Vs/Am} \cdot (500)^2 \cdot {{\pi \cdot (2\cdot 10^{-2} ~\rm m)^2}\over{ 2 \cdot 10^{-2} ~\rm m}} \\ \end{align*}
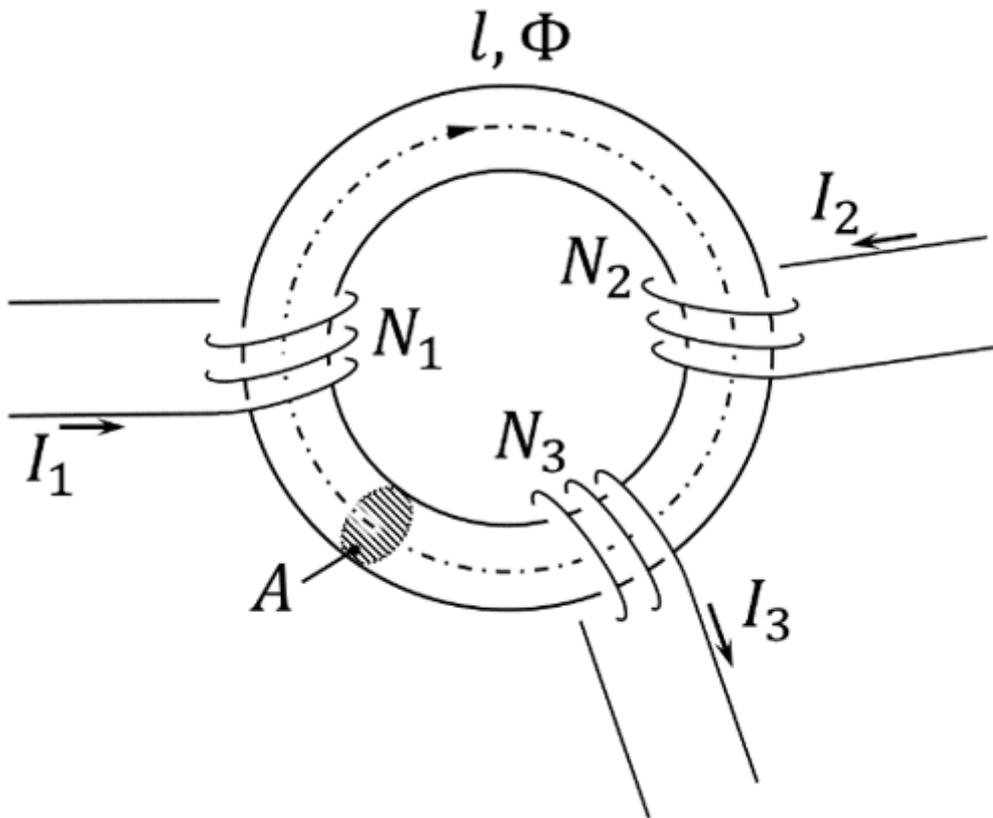
Exercise E16 Magnetic Circuit
(written test, approx. 9 % of a 120-minute written test, SS2024)

1. Calculate the resulting magnetic flux in the iron core.

A toroidal core (ferrite, $\mu_{\rm r}=900$) has a cross-sectional area of $A=300 ~\rm mm^2$ and an average circumference of $l=3 ~\rm dm$.

Result

$R_{\rm m} = 0.884 \cdot 10^{6} \rm {{1}\over{H}} $

$\Phi = 67.8 ~\rm \mu Vs$

Path

The formula of the magnetic resistance is given in voltage-based norms: \begin{align*} R_{\rm m} &= {{l}\over{A}} \cdot {{1}\over{\mu_0 \mu_{\rm r}}} \\ &= {{ 3 \cdot 10^{-1} }\over{ 4 \pi \cdot 10^{-7} {\rm {Vs}\over{Am}} \cdot 900}} \cdot {{1}\over{ 300 \cdot 10^{-6}}} \\ &= 0.884 \cdot 10^{6} ~{{1}\over{H}} \end{align*}

The formula of the magnetic voltage is given in voltage-based norms: \begin{align*} \theta_{\rm R} &= {{\theta}\over{A}} \cdot {{\theta}\over{4\pi \cdot 10^{-7}R}} \theta &= N \cdot I = 300 \cdot 10 \\ &= 300 ~\rm A \end{align*}

To get the flux Φ, the Hopkinson's Law can be applied - similar to the Ohm's Law: \begin{align*} \Phi &= {{\theta_{\rm R} }\over {R_{\rm m}}} \\ &= {{-60~\rm A }\over { 0.884 \cdot 10^{6} \rm {{1}\over{H}} }} \\ &= 67.8 ... \cdot 10^{-6} { \rm A \cdot H} \\ &= 67.8 ... ~\rm \mu Wb \\ &= 67.8 ... ~\rm \mu Vs \\ \end{align*}

On the core, there are three coils with:

- Coil 1: $N_1 = 1200$, $I_1 = 100 ~\rm mA$
- Coil 2: $N_2 = 33$, $I_2 = 3 ~\rm A$
- Coil 3: $N_3 = 270$, $I_3 = 0.3 ~\rm A$

Refer to the drawing for the direction of the windings, current, and flux!

1. Draw the equivalent magnetic circuit that fully represents the setup.
Name all the necessary magnetic resistances, fluxes, and voltages.

Result

- Since the material, and diameter of the core is constant, one can directly simplify the magnetic resistor into a single $R_\rm m$.
- For the orientation of the magnetic voltages θ_1, θ_2, and θ_3, the orientation of the coils and the direction of the current has to be taken into account by the right-hand rule.
- There is only one flux Φ
- The magnetic voltages are antiparallel to the flux for sources and parallel for the load.

$$\...
$$R...
$$\...
$$\...
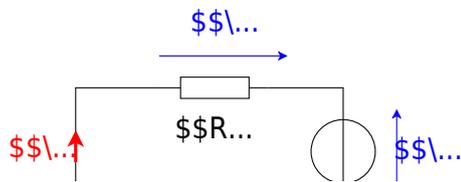
Exercise E18 Magnetic Circuit
(written test, approx. 10 % of a 120-minute written test, SS2024)

3. [illegible] What is the voltage on the ideal capacity C in the shown circuit?

Path

$U_C = 100 ~\rm V$

- $f_r = 39.79 ~\rm MHz$ [illegible] $\underline{Z}_{RLC}$ = 83.0 ~\rm m \Omega$
- $\varphi = 0°$ [illegible] $|\underline{Z}_{RLC}(f_r)| = 20.0 ~\rm m \Omega$

The formula for the resonance frequency f_r is: \begin{align*} f_r &= {{1}\over{2\pi \sqrt{LC}}} \\ &= {{1}\over{2\pi \sqrt{1.6 \cdot 10^{-9} {~\rm H} \cdot 10 \cdot 10^{-9} {~\rm F}}}} \\ &= 39.788... ~\rm MHz \\ \end{align*}

The voltage on the ideal capacity is the input voltage by the Q-factor increased. \begin{align*} U_C &= U_{\rm s} \cdot Q \\ &= U_{\rm s} \cdot \sqrt{ {{L}\over{C}} } \cdot {{1}\over{R}}\\ &= 5 {~\rm V} \cdot \sqrt{ {{ 1.6 \cdot 10^{-9} {~\rm H} }\over{ 10 \cdot 10^{-9} {~\rm F} }} } \cdot {{1}\over{0.020~\Omega}}\\ &= 100 ~\rm V \end{align*}

The impedance at resonance is purely the resistance.
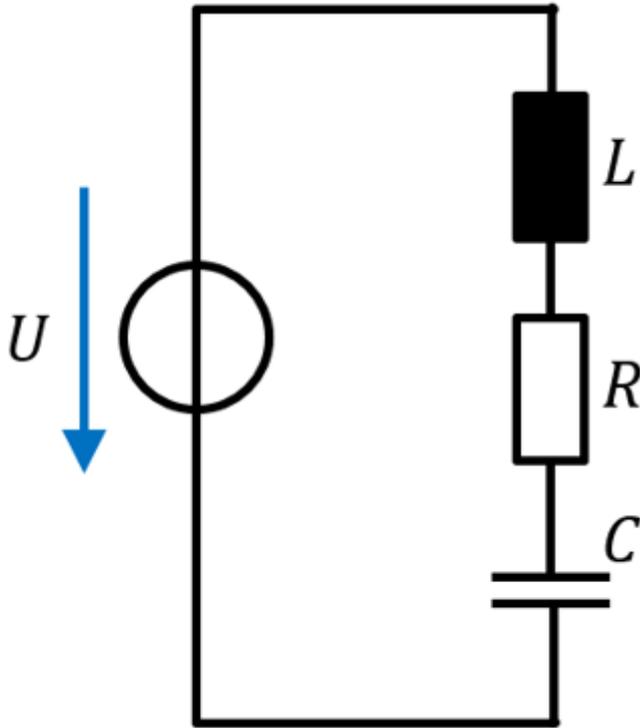
A given capacitor shall have the following values:

- $C=10 ~\rm nF$
- $R=20 ~\rm m\Omega$
- $L=1.6 ~\rm nH$

1. What is the impedance Z_{RLC} of this real capacitor for $f_0=44 ~\rm MHz$? (Phase and magnitude)

Path

The impedance is based on the resistance R and the reactance $X_{LC}= {\rm j}\cdot (X_L - X_C)$:
$$\begin{align*} \underline{Z}_{RLC} &= R + {\rm j}\cdot (X_L - X_C) \\ &= R + {\rm j}\cdot (\omega L - {{1}\over{\omega C}}) \\ &= R + {\rm j}\cdot (2\pi f \cdot L - {{1}\over{2\pi f \cdot C}}) \\ \end{align*}$$

The reactive part is
$$\begin{align*} X_{LC} &= 2\pi f \cdot L - {{1}\over{2\pi f \cdot C}} \\ &= 2\pi 44 \cdot 10^{6} {~\rm MHz} \cdot 1.6 \cdot 10^{-9} {~\rm H} - {{1}\over{2\pi \cdot 10^{6} {~\rm MHz} \cdot 10 \cdot 10^{-9} {~\rm F}}} \\ &= +0.08062... ~\Omega \\ \end{align*}$$
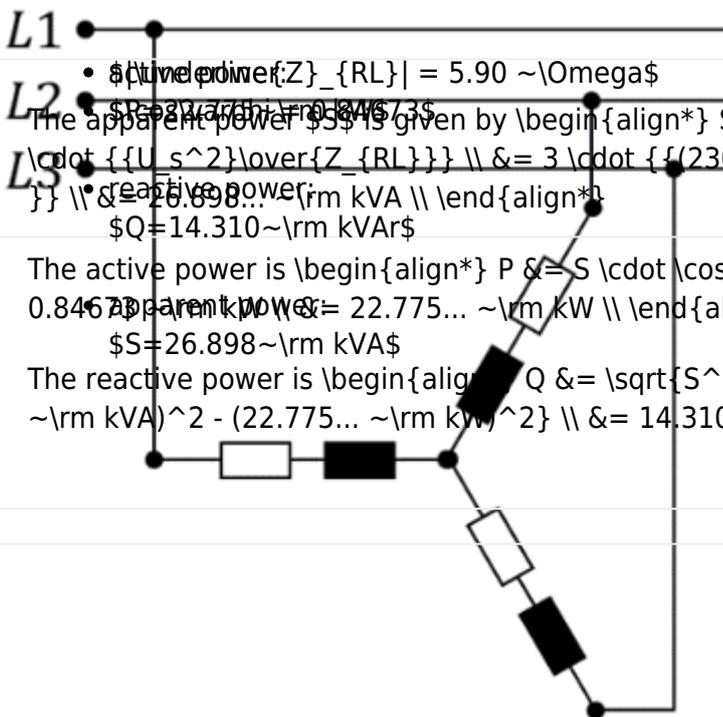
To get the magnitude of the impedance $|\underline{Z}_{RLC}|$ one can use the Pythagorean Theorem:
$$\begin{align*} |\underline{Z}_{RLC}| &= \sqrt{R^2 + X_{LC}^2} \\ &= \sqrt{(0.020~\Omega)^2 + (0.08062... ~\Omega)^2} \\ &= 0.0830 ... ~\Omega \\ \end{align*}$$

For the phase φ the $\arctan$ can be applied:
$$\begin{align*} \varphi &= \arctan \left({{X_{LC}}\over{R}} \right) \\ &= \arctan \left({{0.08062...} \right. \end{align*}$$

~\Omega}\over{0.020 ~\Omega}} \right) \\ &= 1.3276 ... \hat{=} +76° \\
\end{align*}

Exercise E20 Magnetic Circuit
(written test, approx. 10 % of a 120-minute written test, SS2024)

A symmetric and balanced three-phase motor is driven with a $230 ~\rm V$ / $400 ~\rm V$ / $50 ~\rm Hz$ three-phase power net. Each single string has a resistor $R=5 ~\Omega$ and an inductance of $L=10 ~\rm mH$.

Path

1. Calculate the $\cos \varphi$, and the magnitude of the impedance $|Z|$ for a single string.

Path

The phase φ is given by: \begin{align*} \varphi &= \arctan \left({{X_{L}}\over{R}} \right) \\ &= \arctan \left({{2\pi \cdot f \cdot L}\over{R}} \right) \\ &= \arctan \left({{2\pi \cdot 50 {~\rm Hz} \cdot 10 \cdot 10^{-3} {~\rm H}}\over{5 ~\Omega}} \right) \\ &= 0.5609 ... \hat{=} +32° \\ \end{align*}

With this, the $\cos \varphi$ becomes \begin{align*} \cos \varphi &= \cos(0.5609 ...) \\ &= 0.84673...\\ \end{align*}

2. Calculate the apparent, active, and the reactive power, and the with a power of the motor.

Result

- $\cos \varphi = 0.84673$
- active power:
  $P=22.775 ~\rm kW$
- reactive power:
  $Q=14.310~\rm kVAr$
- Apparent power:
  $S=26.898~\rm kVA$

$|{Z}_{RL}| = 5.90 ~\Omega$

The apparent power S is given by \begin{align*} S &= 3 \cdot U_s \cdot I_s \\ &= 3 \cdot {{U_s^2}\over{Z_{RL}}} \\ &= 3 \cdot {{(230~\rm V)^2}\over{ 5.90 ~\Omega }} \\ &= 26.898... ~\rm kVA \\ \end{align*}

The active power is \begin{align*} P &= S \cdot \cos \varphi \\ &= 26.898... \cdot 0.84673 ... \\ &= 22.775... ~\rm kW \\ \end{align*}

The reactive power is \begin{align*} Q &= \sqrt{S^2 - P^2} \\ &= \sqrt{ (26.898... ~\rm kVA)^2 - (22.775... ~\rm kW)^2} \\ &= 14.310...~\rm kVAr \\ \end{align*}

The impedance is given by: \begin{align*} |\underline{Z}_{RL}| &= \sqrt{X_{L}^2 + R^2} \\ &= \sqrt{(2\pi \cdot f \cdot L)^2 + R^2} \\ &= \sqrt{(2\pi \cdot 50 {~\rm Hz} \cdot 10 \cdot 10^{-3} {~\rm H})^2 +(5 ~\Omega)^2} \\ &= 5.905... ~\Omega\\ \end{align*}