

# Exam Winter Semester 2022

## Student Group

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# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

## Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Tasks

### Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wires with a temperature of  $180^\circ\text{C}$ . The electric

power dissipation (= heat flow) of  $P=40\text{ W}$  is necessary.

Calculate the current  $I$  needed to operate for heating elements.

The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6}\ \Omega\text{ m}$ .

The heating element is  $3\text{ m}$  long and has a diameter of  $3.57\text{ mm}$ .

Calculate the resistance  $R$  of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ I &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{ W}}{0.33\ \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \quad \text{with } A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \& \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \& \quad R = \\ &= 1.10 \cdot 10^{-6}\ \Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

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[resistivity, power, exam ee1 ws2022](#)

**Exercise E1 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A thermistor is used as a temperature sensor in a refrigeration system. The thermistor has a resistance of  $10 \text{ k}\Omega$  at  $25^\circ\text{C}$ . Its temperature coefficients are:  $\alpha = 0.01 \text{ K}^{-1}$  and  $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$ .

Result: The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Calculate the resistance of the thermistor at  $-40^\circ\text{C}$ .

The power transferred to the load of the circuit and of the heat therefore, a solution is to increase the resistance of the thermistor. Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

$$\Delta T = T_{\text{end}} - T_{\text{start}}$$

$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

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[temperature dependent resistance](#), [power](#), [heat](#), [exam ee1 ws2022](#)

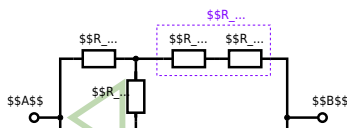
**Exercise E2 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following circuit is given with  $R_1 = 20 \text{ }\Omega$ ,  $R_2 = 10 \text{ }\Omega$ ,  $R_3 = 15 \text{ }\Omega$  and the voltage  $U = 10 \text{ V}$ . Calculate the current  $I$  through the resistor  $R_3$ .

Solution

$$R_{\text{eq}} = 13.8 \text{ }\Omega$$

Now a wye-delta transformation is necessary.

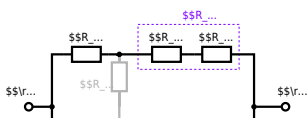


Since  $R_2=R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series: 
$$R_{eq} = R_Y + (R_Y + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \Omega + 200 \Omega + 200 \Omega) \parallel (100 \Omega + 100 \Omega) \parallel R_{\text{eq}} = (500 \Omega) \parallel (200 \Omega) \parallel R_{\text{eq}} = \frac{500 \Omega \cdot 200 \Omega}{500 \Omega + 200 \Omega} \parallel$$

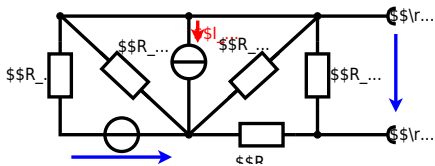
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[network simplification, exam ee1 ws2022](#)

**Exercise E3 Equivalent linear Source  
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
Result

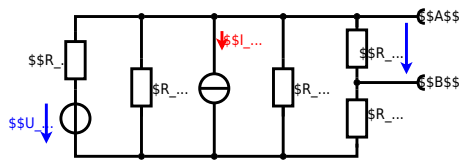
$$U_{\text{s}} = U_{\text{AB}} = 4.5 \text{ V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \Omega$$



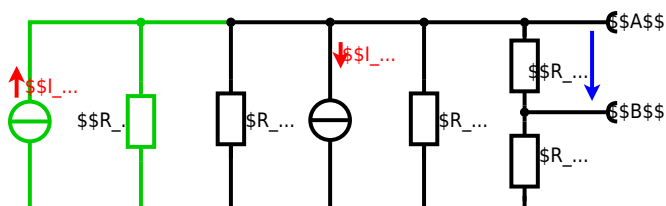
Calculate the internal resistance  $R_{int}$  and the source voltage  $U_s$  of an equivalent linear voltage source on the connectors  $A$  and  $B$ .  $R_1=5.0 \Omega$ ,  $U_2=6.0 \text{ V}$ ,  $R_3=10 \Omega$ ,  $I_4=4.2 \text{ A}$ ,  $R_5=10 \Omega$ ,  $R_6=7.5 \Omega$ ,  $R_7=15 \Omega$ . Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_{24}}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following:

$$U_{24}$$

$$U_{AB} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ .

Therefore the voltage between  $A$  and  $B$  is given as:

$$U_{AB} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$ :

$$U_{AB} = \left( \frac{6.0V}{5.0\Omega} - 4.2\Omega \right) \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega}$$

$$R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

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dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

**Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)**

The circuit below (reproduced from the exam) consists of a  $10V$  DC voltage source, a  $20\Omega$  resistor, a  $2\mu F$  capacitor, and a switch  $S_1$ . The switch is open. The voltage across the capacitor is again  $0V$  at the moment  $t_0=0s$  when the switch  $S_1$  is closed. Calculate the voltage  $u_c(t_2)$  across the capacitor at  $t_2=1ms$  after closing the switch.

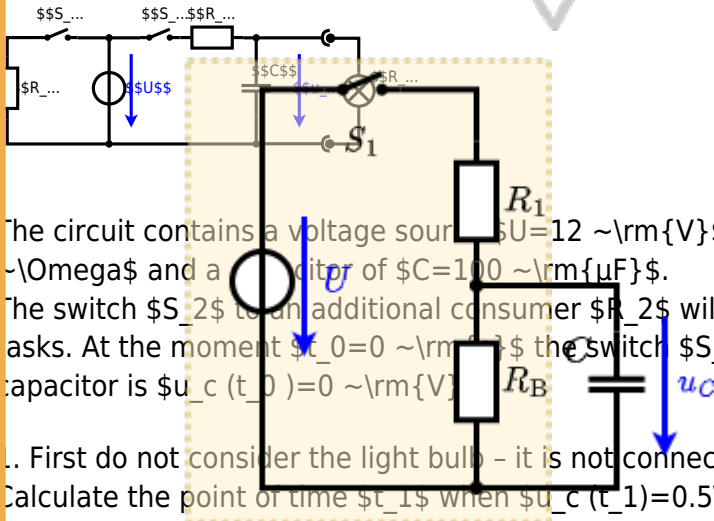
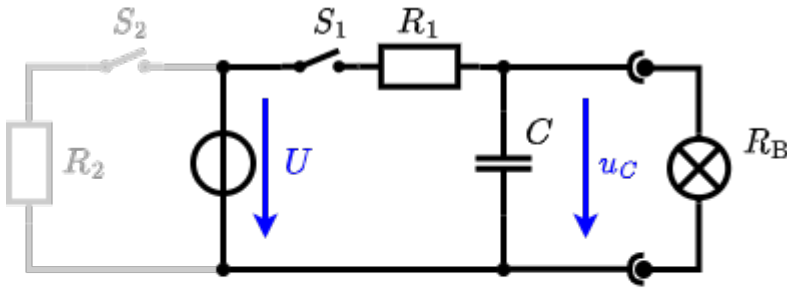
**Result:** To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_2$ .

$$U_{\Delta} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{10V \cdot 20\Omega}{20\Omega + 20\Omega} = 5V$$

**Solution:** The internal resistance  $R_i$  is given by substituting the ideal voltage source with its internal resistance  $R_2$ .

$$R_i = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{20\Omega \cdot 20\Omega}{20\Omega + 20\Omega} = 10\Omega$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .



The circuit contains a voltage source  $U=12 \text{ V}$ , a switch  $S_1$ , a resistor of  $R_1=20 \text{ }\Omega$  and a capacitor of  $C=100 \text{ }\mu\text{F}$ . The switch  $S_2$  to an additional consumer  $R_2$  will be considered to be open for the first tasks. At the moment  $t_0=0 \text{ s}$  the switch  $S_1$  is closed, the voltage across the capacitor is  $u_c(t_0)=0 \text{ V}$ .

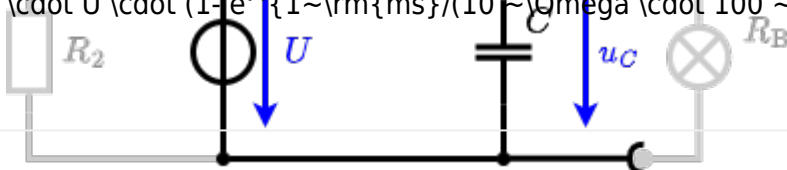
... First do not consider the light bulb - it is not connected to the RC circuit.  
 Calculate the point of time  $t_1$  when  $u_c(t_1)=0.5 \cdot U$ .

An equivalent linear voltage source can be given with  $U_s$ ,  $R_1$ , and  $R_{\text{B}}$  as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:  $U_s = U \cdot \frac{R_{\text{B}}}{R_1 + R_{\text{B}}} = 1/2 \cdot U$  The internal resistance is given by substituting the ideal voltage source with its resistance ( $R=0 \text{ }\Omega$ , short-circuit).

$$R_i = R_1 \parallel R_{\text{B}} = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms}/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$



So, here only  $R_1$  and  $C$  gives the time constant:  $\tau = R_1 \cdot C$

The following formula describes the time course of  $u_C(t)$  which has to be  $u_c(t_1)=0.5 \cdot U$ :

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to  $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

**Exercise E4 Analyzing complex Impedances**  
(written test, approx. 14 % of a 60-minute written test, WS2022)

2. A circuit has the nodes and impedances shown in the figure. The voltage  $V$  is 50 V (rms) and the current  $I$  is 0.24 A (rms). The resistor  $R_1$  shall be given.

After analysis, the full bidirectional current impedance values extracted and digitized in the table. The table is given in the following format.

.. The table contains physical values of the components.

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} \quad \&= \{ \{ 50 \}$$
  
The voltage  $V$  is 50 V (rms) and the current  $I$  is 0.24 A (rms). The resistor  $R_1$  shall be given.  
resulting impedance  $Z = \frac{U}{I} = \frac{50}{0.24} = 208.33 \Omega$   
Therefore, the component  $R_1$  is a capacitor with the same absolute value of 208.33  $\Omega$ .  
$$\underline{Z} = R_1 + j\omega L + \frac{1}{j\omega C} = R_1 + j\omega L - \frac{1}{\omega C}$$
  
The phase  $\varphi$  can be calculated as  $\varphi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-4.68}{0.24}\right)$   
With the complex part comes the physical value  $X_L = \omega L$   
$$\&= \{ \{ X_L \} \over{2\pi \cdot f} \} \quad \&= \{ \{ 4.68 \} \over{2\pi \cdot 300} \}$$
  
The phase  $\varphi$  can be calculated as  $\varphi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-4.68}{0.24}\right)$

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complex impedance, exam ee1 ws2022

**Exercise E1 Impedances at different Frequencies**  
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A circuit has the resistors and impedances shown in the figure. The voltage  $V$  is 50 V (rms) and the current  $I$  is 0.24 A (rms). The resistor  $R_1$  shall have the same absolute value of the impedance as a capacitor  $C_1 = 40 \text{ nF}$  at  $f_1 = 4 \text{ MHz}$ .

Solution  
Solution  $R_1 = 1.00 \Omega$   
Solution  $R_2 = 10.0 \Omega$

A series circuit means that the current is constant on every component.  
 The equivalent impedance for the parallel combination of  $R_2$  and  $R_3$  is given by  $Z_{eq} = \frac{1}{\frac{1}{R_2} + \frac{1}{R_3}}$ .  
 The voltage across the parallel combination is  $V_{eq} = I \cdot Z_{eq}$ .  
 The current through  $R_2$  is  $I_2 = \frac{V_{eq}}{R_2}$ .  
 The current through  $R_3$  is  $I_3 = \frac{V_{eq}}{R_3}$ .  
 The total current is  $I = I_2 + I_3$ .  
 The voltage across  $R_1$  is  $V_1 = I \cdot R_1$ .  
 The voltage across the parallel combination is  $V_{eq} = I \cdot Z_{eq}$ .  
 The total voltage is  $V = V_1 + V_{eq}$ .  
 The total current is  $I = \frac{V}{Z_{total}}$ .  
 The total impedance is  $Z_{total} = R_1 + Z_{eq}$ .  
 The total current is  $I = \frac{V}{R_1 + Z_{eq}}$ .  
 The voltage across  $R_1$  is  $V_1 = I \cdot R_1$ .  
 The voltage across the parallel combination is  $V_{eq} = I \cdot Z_{eq}$ .  
 The current through  $R_2$  is  $I_2 = \frac{V_{eq}}{R_2}$ .  
 The current through  $R_3$  is  $I_3 = \frac{V_{eq}}{R_3}$ .  
 The total current is  $I = I_2 + I_3$ .  
 The voltage across  $R_1$  is  $V_1 = I \cdot R_1$ .  
 The voltage across the parallel combination is  $V_{eq} = I \cdot Z_{eq}$ .  
 The total voltage is  $V = V_1 + V_{eq}$ .  
 The total current is  $I = \frac{V}{Z_{total}}$ .  
 The total impedance is  $Z_{total} = R_1 + Z_{eq}$ .  
 The total current is  $I = \frac{V}{R_1 + Z_{eq}}$ .

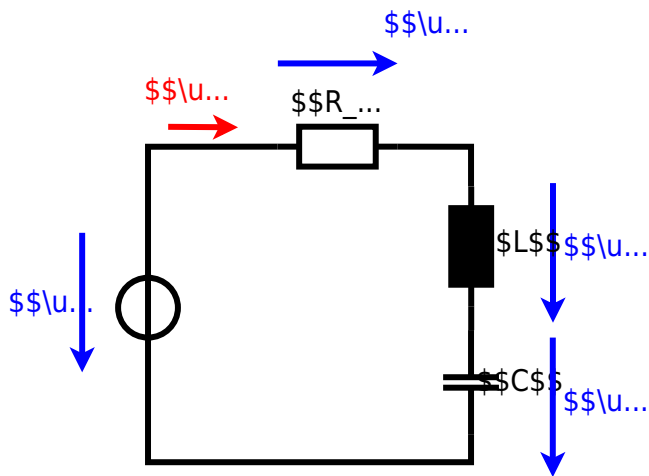
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[complex impedance, exam ee1 ws2022](#)

**Exercise E1 Complex Impedance Circuit**  
**(written test, approx. 15 % of a 60-minute written test, WS2022)**

1. Consider the circuit below. The voltage source is  $v_s(t) = 3.0 \cos(2\pi \cdot 15 \cdot t)$  V. The circuit consists of a voltage source  $v_s(t) = 3.0 \cos(2\pi \cdot 15 \cdot t)$  V, a resistor  $R = 10 \Omega$ , an inductor  $L = 330 \mu\text{H}$ , and a capacitor  $C = 0.22 \mu\text{F}$ , all in series.  
 Solution

Result  $Z = 19.73 \Omega$   
 Draw the circuit diagram of the given circuit.  
 Label all components, voltages, and currents.  
 $Z = \frac{V}{I}$   
 $Z_C = \frac{1}{j\omega C}$   
 Result  $Z = 19.73 \Omega$   
 With  $f = 15 \text{ kHz}$   
 $Z_C = \frac{1}{j\omega C}$   
 $Z_L = j\omega L$   
 $Z = R + Z_L + Z_C$   
 $Z = R + j\omega L - \frac{1}{j\omega C}$   
 $Z = \sqrt{R^2 + (\omega L - \frac{1}{\omega C})^2}$





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