

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 and an electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary. Calculate the current I needed to operate it.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ I &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \text{with } R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

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[resistivity, power, exam ee1 ws2022](#)

Exercise E3 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, explains a thermistor's resistance in a refrigeration system. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: Calculate the resistance of the thermistor at -40°C .

Solution: $R = 6.5 \text{ k}\Omega$

The power transfer is reduced by a factor of 10. Therefore, a solution is to use a heat sink.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

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\begin{align*} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) && | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} && \\ R &= 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right) && \\ &= 6.5 \text{ k}\Omega && \end{align*}
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[temperature dependent resistance](#), [power](#), [heat](#), [exam ee1 ws2022](#)

Exercise E1 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

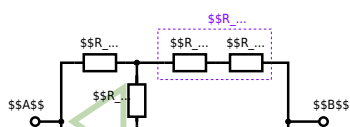
The following circuit is given. $R_1 = 10 \text{ }\Omega$, $R_2 = 20 \text{ }\Omega$, $R_3 = 30 \text{ }\Omega$, $R_4 = 40 \text{ }\Omega$, $R_5 = 50 \text{ }\Omega$, $R_6 = 60 \text{ }\Omega$, $R_7 = 70 \text{ }\Omega$, $R_8 = 80 \text{ }\Omega$, $R_9 = 90 \text{ }\Omega$, $R_{10} = 100 \text{ }\Omega$.

Result: $R_{\text{eq}} = 132.8 \text{ }\Omega$

Solution

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\begin{align*} R_{\text{eq}} &= 132.8 \text{ }\Omega && \end{align*}
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Now a wye-delta transformation is necessary.

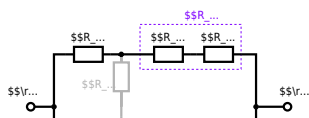


Since $R_2=R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel R_{\text{eq}} = (500 \sim \Omega) \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \frac{500 \sim \Omega \cdot 200 \sim \Omega}{500 \sim \Omega + 200 \sim \Omega}$$

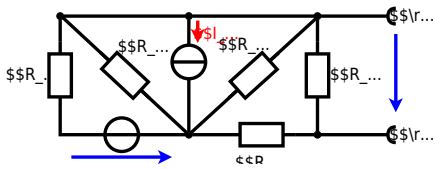
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[network simplification, exam ee1 ws2022](#)

**Exercise E2 Equivalent linear Source
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.
Result

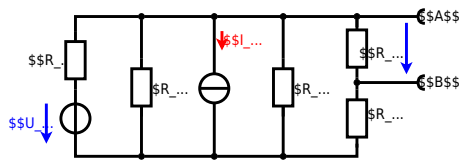
$$U_{\text{S}} = U_{\text{AB}} = 4.5 \text{ V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \sim \Omega$$



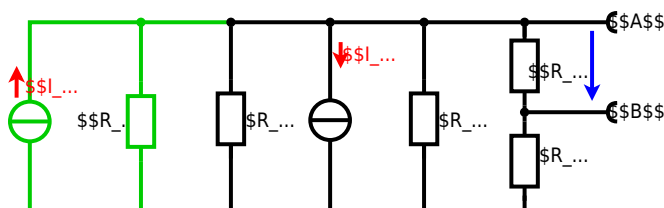
Calculated the internal resistance R_{int} and the source voltage U_{oc} of an equivalent linear voltage source on the connectors A and B . $R_1=5.0 \text{ } \Omega$, $U_2=6.0 \text{ V}$, $R_3= 10 \text{ } \Omega$, $I_4=4.2 \text{ A}$, $R_5=10 \text{ } \Omega$, $R_6=7.5 \text{ } \Omega$, $R_7=15 \text{ } \Omega$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{56}$$

$$I_{24} = \frac{U_{24}}{R_1 + R_3 + R_5} = \frac{6.0 \text{ V} - 4.2 \text{ V}}{5.0 \text{ } \Omega + 10 \text{ } \Omega + 10 \text{ } \Omega} = 0.25 \text{ A}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 + R_3 + R_5} = \frac{6.0 \text{ V} - 4.2 \text{ V}}{5.0 \text{ } \Omega + 10 \text{ } \Omega + 10 \text{ } \Omega} \cdot \frac{15 \text{ } \Omega \cdot 2.5 \text{ } \Omega}{7.5 \text{ } \Omega + 15 \text{ } \Omega + 2.5 \text{ } \Omega} = 15 \text{ V} \cdot \frac{1}{7.5 + 2.5} = 1.5 \text{ V}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0 \text{ } \Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5) = 2.5 \text{ } \Omega \parallel (10 \text{ } \Omega + 5 \text{ } \Omega) = 2.5 \text{ } \Omega \parallel 15 \text{ } \Omega = 2.14 \text{ } \Omega$$

with $R_1 \parallel R_3 \parallel R_5 = 5 \text{ } \Omega \parallel 10 \text{ } \Omega \parallel 10 \text{ } \Omega = 5 \text{ } \Omega \parallel 5 \text{ } \Omega = 2.5 \text{ } \Omega$:

$$U_{AB} = \frac{6.0 \text{ V} - 4.2 \text{ V}}{5.0 \text{ } \Omega} \cdot \frac{15 \text{ } \Omega \cdot 2.5 \text{ } \Omega}{7.5 \text{ } \Omega + 15 \text{ } \Omega + 2.5 \text{ } \Omega} = 1.5 \text{ V}$$

$$R_{AB} = 15 \text{ } \Omega \parallel (7.5 \text{ } \Omega + 2.5 \text{ } \Omega) = 2.14 \text{ } \Omega$$

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dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)

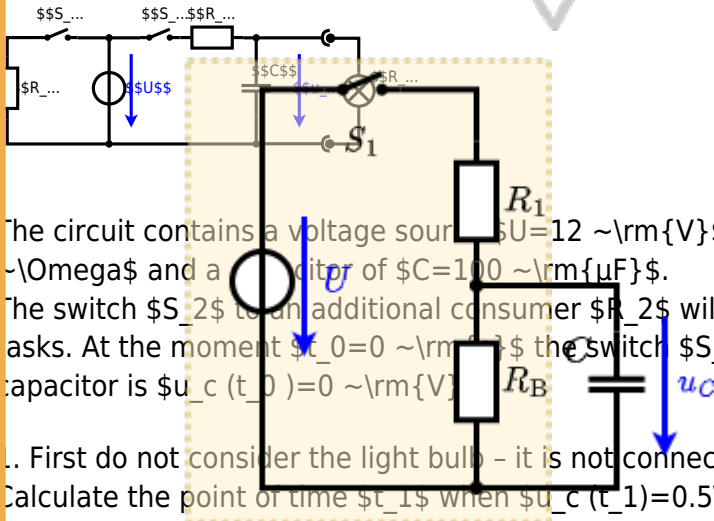
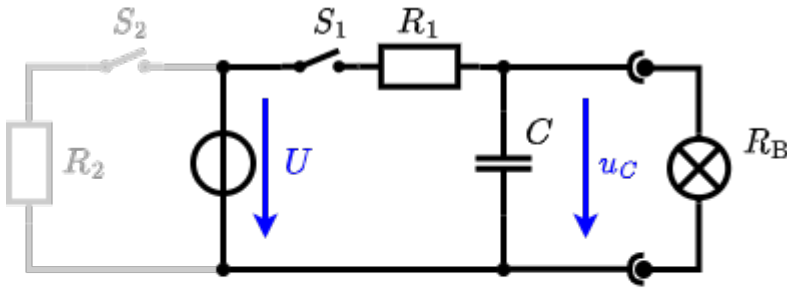
The circuit (with the ideal battery) also consists of $R_1 = 6 \text{ } \Omega$, $R_2 = 20 \text{ } \Omega$, and a capacitor $C = 2 \text{ } \mu\text{F}$ as indicated in Figure 1. The switch S_1 is open. The voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Result: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\Delta} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12 \text{ V} \cdot 20 \text{ } \Omega}{6 \text{ } \Omega + 20 \text{ } \Omega} = 4.71 \text{ V}$$

Solution: The internal voltage source U_{Δ} and the voltage U are independent of the capacitor. $U_{\Delta} = 4.71 \text{ V}$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

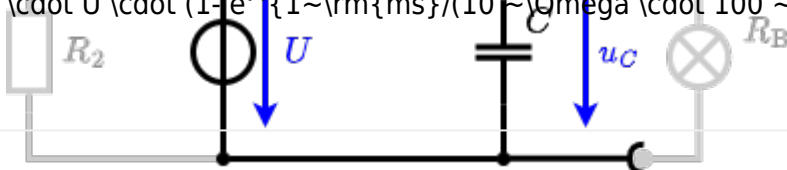


The circuit contains a voltage source $U=12 \text{ V}$, a switch S_1 , a resistor of $R_1=20 \text{ }\Omega$ and a capacitor of $C=100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0=0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0 \text{ V}$.
 ... First do not consider the light bulb - it is not connected to the RC circuit.
 Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

An equivalent linear voltage source can be given with U_s , R_1 , and R_{B} as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_{\text{B}}}{R_1 + R_{\text{B}}} = 1/2 \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($r=0 \text{ }\Omega$, short-circuit).
 $R_i = R_1 \parallel R_{\text{B}} = 10 \text{ }\Omega$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms}/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:
 $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E1 Analyzing complex Impedances
(written test, approx. 14 % of a 60-minute written test, WS2022)

A circuit has the nodes and impedances shown in the figure. The voltage V and the current I through the components (R_1 and X_1) shall be given.

After analysis, the full bi-dimensional complex impedance values extracted and digitized in handwritten LaTeX are $Z = (2 - j4) \Omega$ and $Z = (5 + j2) \Omega$.

.. Calculate the physical values of the two components.
 Solution $R_1 = 2 \Omega$ and $X_1 = -4 \Omega$

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} \quad \&= \{ \{ 50 \}$$

 The voltage V and current I through the components (R_1 and X_1) shall be given.
 resulting impedance $Z = (2 - j4) \Omega$ and $Z = (5 + j2) \Omega$.
 Therefore, the component R_1 has a value of 2Ω and the capacitor X_1 has a value of -4Ω .

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{(2 - j4) \Omega} = \frac{50 \angle 0^\circ}{\sqrt{2^2 + 4^2} \angle -63.4^\circ} = \frac{50 \angle 0^\circ}{4.47 \angle -63.4^\circ} = 11.18 \angle 63.4^\circ \text{ A}$$

$$\underline{V} = \underline{I} \cdot \underline{Z} = 11.18 \angle 63.4^\circ \cdot (2 - j4) \Omega = 22.36 \angle 63.4^\circ - 44.72 \angle 26.6^\circ = 22.36 \cos(63.4^\circ) - j44.72 \sin(63.4^\circ) + j22.36 \sin(63.4^\circ) + 44.72 \cos(26.6^\circ)$$

$$\underline{V} = 22.36 \cdot 0.447 - j44.72 \cdot 0.894 + j22.36 \cdot 0.894 + 44.72 \cdot 0.894 = 10.11 - j40.0 + j20.0 + 40.0 = 50.11 - j20.0 \text{ V}$$

 With the complex part comes the physical values $R_1 = 2 \Omega$ and $X_1 = -4 \Omega$.

$$\&= \{ \{ X_L \} \over {2\pi \cdot f} \} \&= \{ \{ 4.68 \sim \Omega \} \over {2\pi \cdot 300} \}$$

 The phase φ can be calculated as
$$\varphi_i = \arctan \left(\frac{\text{Im}()}{\text{Re}()} \right) = \arctan \left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega} \right)$$

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 complex impedance, exam ee1 ws2022

Exercise E9 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

A circuit has the resistors $R_1 = 1 \text{ k}\Omega$ and $R_2 = 10 \text{ k}\Omega$ and a capacitor $C_1 = 40 \text{ nF}$ at $f = 4 \text{ MHz}$. The voltage V and the current I through the resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f = 4 \text{ MHz}$.

Solution
 Solution $R_1 = 1.00 \sim \Omega$
 Solution $R_2 = 10.0 \sim \Omega$

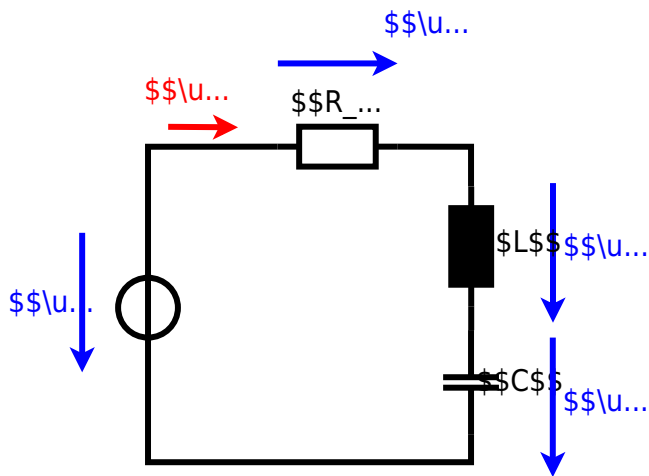
A series circuit means that the current is constant on every component.
 The equivalent resistance for the parallel combination is given by $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$.
 Since the current is constant, the voltage across each component is the same. The voltage across the parallel combination is $V_{parallel} = I_{total} \cdot R_{eq}$.
 The voltage across the series resistor is $V_{series} = I_{total} \cdot R_3$.
 The total voltage is $V_{total} = V_{parallel} + V_{series} = I_{total} \cdot R_{eq} + I_{total} \cdot R_3 = I_{total} \cdot (R_{eq} + R_3)$.
 Therefore, the resulting current of the parallel circuit is given as $I_{total} = \frac{V_{total}}{R_{eq} + R_3}$.
 The voltage across the parallel combination is $V_{parallel} = I_{total} \cdot R_{eq} = \frac{V_{total} \cdot R_{eq}}{R_{eq} + R_3}$.
 The current through the parallel combination is $I_{parallel} = \frac{V_{parallel}}{R_{eq}} = \frac{V_{total}}{R_{eq} + R_3}$.
 The current through the series resistor is $I_{series} = \frac{V_{series}}{R_3} = \frac{I_{total} \cdot R_3}{R_3} = I_{total}$.
 The total current is $I_{total} = \frac{V_{total}}{R_{eq} + R_3}$.

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Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Consider the circuit below. The voltage source is $u(t) = 3.0 \sin(2\pi \cdot 15 \cdot t)$ V. The circuit consists of a resistor of 10Ω , an inductor of $330 \mu\text{H}$, and a capacitor of $0.22 \mu\text{F}$, all in series.
 Solution

Result $Z = 19.8 - j31.4 \Omega$
 Draw the circuit diagram of the given circuit with all components, voltages, and currents.
 $Z = \frac{U}{I}$
 $Z_C = \frac{1}{2\pi \cdot f \cdot C} = \frac{1}{2\pi \cdot 15 \cdot 0.22 \cdot 10^{-6}} = 19.8 \text{ kHz}$
 $Z_L = 2\pi \cdot f \cdot L = 2\pi \cdot 15 \cdot 330 \cdot 10^{-6} = 31.4 \text{ kHz}$
 $\underline{Z} = R + \underline{Z}_L + \underline{Z}_C = R + j \cdot Z_L - Z_C = R + j \cdot (Z_L - Z_C) = \sqrt{R^2 + (\underline{Z}_L - \underline{Z}_C)^2}$



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