

# Exam Winter Semester 2022

## Student Group

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# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

## Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Only EEE1-relevant Part

This part is only for about 20..25 minutes !

### Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The heating element made of nichrome wire with a temperature coefficient of  $1.80 \cdot 10^{-4} \text{ K}^{-1}$  Electric power dissipation (= heat flow) of  $P=40 \text{ W}$  is necessary.

Calculate the current  $I$  needed to operate it for heating elements.

The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$ .

The heating element is  $3 \text{ m}$  long and has a diameter of  $3.57 \text{ mm}$ .

∴ Calculate the resistance  $R$  of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad || \quad R = \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad || \quad R = \\ &= 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

**Exercise E3 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. The diagram explains why the effect of constant resistance on refrigeration system structure is not as simple as it seems. The refrigerator has a resistance of  $10 \text{ k}\Omega$  at  $25^\circ\text{C}$ . Your answer.

Its temperature coefficients are:  $\alpha = 0.01 \text{ } \frac{1}{\text{K}}$  and  $\beta = 71 \cdot 10^{-6} \text{ } \frac{1}{\text{K}^2}$

Result: The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Calculate the resistance of the thermostat at  $-40^\circ\text{C}$ .

The power transfered to the load of the circuit and of the heater is therefore, a solution is to use a thermostat that floats up the refrigeration system.

Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

with  $\Delta T = T_{\text{end}} - T_{\text{start}}$

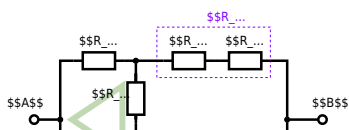
$$R = 10 \text{ k}\Omega \cdot (1 + 0.01 \frac{1}{\text{K}} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \frac{1}{\text{K}^2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2)$$

**Exercise E1 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall be used:  $R_1 = 20 \text{ k}\Omega$ ,  $R_2 = R_3 = 10 \text{ k}\Omega$  and the source  $U = 10 \text{ V}$ .  
 Result:  $R_{\text{eq}} = 13.8 \text{ k}\Omega$ .

Solution  
 $R_{\text{eq}} = 13.8 \text{ k}\Omega$

Now a wye-delta transformation is necessary.

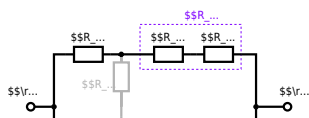


Since  $R_2=R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series: 
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between A and B.

Solution



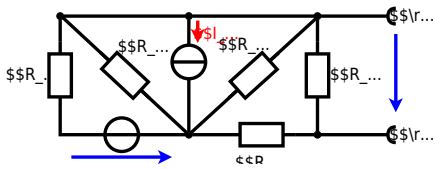
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_{-1}) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \Omega + 200 \Omega + 200 \Omega) \parallel (100 \Omega + 100 \Omega) \parallel R_{\text{eq}} = (500 \Omega) \parallel (200 \Omega) \parallel R_{\text{eq}} = \frac{500 \Omega \cdot 200 \Omega}{500 \Omega + 200 \Omega} \parallel R_{\text{eq}}$$

**Exercise E2 Equivalent linear Source  
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
Result

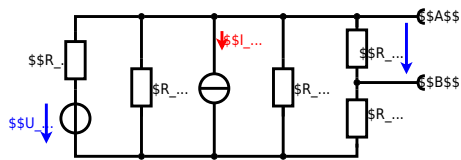
$$U_{\text{s}} = U_{\text{AB}} = 4.5 \text{ V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \Omega$$



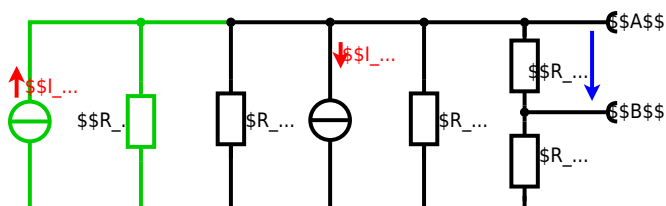
Calculate the internal resistance  $R_{int}$  and the source voltage  $U_s$  of an equivalent linear voltage source on the connectors  $A$  and  $B$ .  
 $R_1 = 5.0 \Omega$ ,  $U_2 = 6.0 \text{ V}$ ,  $R_3 = 10 \Omega$ ,  $I_4 = 4.2 \text{ A}$ ,  
 $R_5 = 10 \Omega$ ,  $R_6 = 7.5 \Omega$ ,  $R_7 = 15 \Omega$   
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_{24}}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following:

$$U_{24}$$

$$I = R_{135} \cdot I_{24} \quad I = \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ .

Therefore the voltage between  $A$  and  $B$  is given as:

$$U_{AB} = U_{24} \cdot \left\{ \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right\} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot \left\{ \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right\}$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with  $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$ :

$$U_{AB} = \left( \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \right) \cdot \left\{ \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \right\} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

### Full Exam

These is the full exam

Full exam

### Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

The heating element made of nichrome wire with a cross-section of  $1.80\text{mm}^2$ . Each second, a power dissipation (= heat flow) of  $P=40\text{W}$  is necessary. Determine the current  $I$  needed to operate for heating elements. The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6}\Omega\text{m}$ . The heating element is  $3\text{m}$  long and has a diameter of  $3.57\text{mm}$ . Calculate the resistance  $R$  of the heating element.

Solution

$$P = U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{W}}{0.33\Omega}}$$

$$R = \rho \cdot \frac{l}{A} \quad | \quad A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad R = \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad R = 1.10 \cdot 10^{-6}\Omega\text{m} \cdot \frac{4 \cdot l}{d^2 \cdot \pi}$$

$$3 \cdot 10^{-3} \cdot \pi \cdot R^2$$

[electrical\\_engineering\\_and\\_electronics:task\\_rj0r6j4apumukrj6\\_with\\_calculation](#)  
[resistivity, power, exam ee1 ws2022](#)

**Exercise E3 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A refrigerator is equipped with a heating element to melt ice. The element is made of a material with a temperature coefficient of resistance  $\alpha = 0.01 \text{ K}^{-1}$  and  $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$ . The resistance of the element is  $R_0 = 6.5 \text{ k}\Omega$  at  $25^\circ\text{C}$ .

Its temperature coefficients are:  $\alpha = 0.01 \text{ K}^{-1}$  and  $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$ .

**Result**  
 The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Calculate the resistance of the filament at  $-40^\circ\text{C}$ .

The power transferred to the heating element is  $P = \frac{U^2}{R}$ .  
 The current through the filament is  $I = \frac{U}{R}$ .  
 Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

$$R = 6500 \cdot (1 + 0.01 \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2)$$

[electrical\\_engineering\\_and\\_electronics:task\\_70jg4yzznocarsq\\_with\\_calculation](#)  
[temperature dependent resistance, power, heat, exam ee1 ws2022](#)

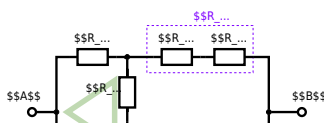
**Exercise E1 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall hold:  $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 15 \text{ k}\Omega$ ,  $R_3 = 10 \text{ k}\Omega$ ,  $R_4 = 10 \text{ k}\Omega$ ,  $R_5 = 10 \text{ k}\Omega$ ,  $R_6 = 10 \text{ k}\Omega$ ,  $R_7 = 10 \text{ k}\Omega$ ,  $R_8 = 10 \text{ k}\Omega$ ,  $R_9 = 10 \text{ k}\Omega$ ,  $R_{10} = 10 \text{ k}\Omega$ ,  $R_{11} = 10 \text{ k}\Omega$ ,  $R_{12} = 10 \text{ k}\Omega$ ,  $R_{13} = 10 \text{ k}\Omega$ ,  $R_{14} = 10 \text{ k}\Omega$ ,  $R_{15} = 10 \text{ k}\Omega$ ,  $R_{16} = 10 \text{ k}\Omega$ ,  $R_{17} = 10 \text{ k}\Omega$ ,  $R_{18} = 10 \text{ k}\Omega$ ,  $R_{19} = 10 \text{ k}\Omega$ ,  $R_{20} = 10 \text{ k}\Omega$ .

**Solution**

$$R_{\text{eq}} = 132.8 \text{ k}\Omega$$

Now a wye-delta transformation is necessary.



Since  $R_2 = R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as:

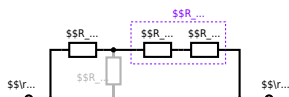
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel (R_Y + R_2 + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between  $A$  and  $B$ .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

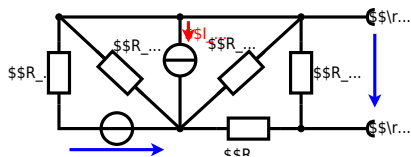
$$R_{\text{eq}} = (R_2 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

[electrical\\_engineering\\_and\\_electronics:task\\_x357drkaqv84jnsc\\_with\\_calculation\\_network\\_simplification,\\_exam\\_ee1\\_ws2022](#)

**Exercise E2 Equivalent linear Source  
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
Result

$$U_{\text{S}} = U_{\text{AB}} = 4.5 \, \text{V} \parallel R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



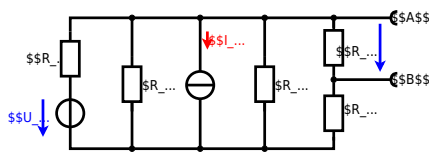
Calculate the internal resistance  $R_i$  and the source voltage  $U_s$  of an equivalent linear voltage source on the connectors A and B.

$R_1=5.0 \Omega$ ,  $U_2=6.0 \text{ V}$ ,  $R_3= 10 \Omega$ ,  $I_4=4.2 \text{ A}$ ,  
 $R_5=10 \Omega$ ,  $R_6=7.5 \Omega$ ,  $R_7=15 \Omega$

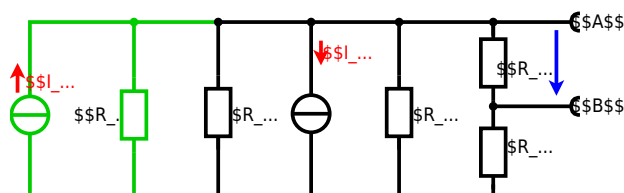
Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in

parallel, like also  $I_2$  and  $I_4$ : 
$$R_{135} = R_1 || R_3 || R_5$$
 
$$I_{24} = I_2 - I_4 = \left\{ \frac{U_2}{R_1} \right\} - I_4$$
 The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following: 
$$U_{24} = R_{135} \cdot I_{24} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ . Therefore the voltage between  $A$  and  $B$  is given as: 
$$U_{\text{AB}} = U_{24} \cdot \left\{ \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right\} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot \left\{ \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \right\}$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit): 
$$R_{\text{AB}} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$ :

$$U_{\text{AB}} = \left\{ \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \right\} \cdot \left\{ \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \right\} || R_{\text{AB}} = 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

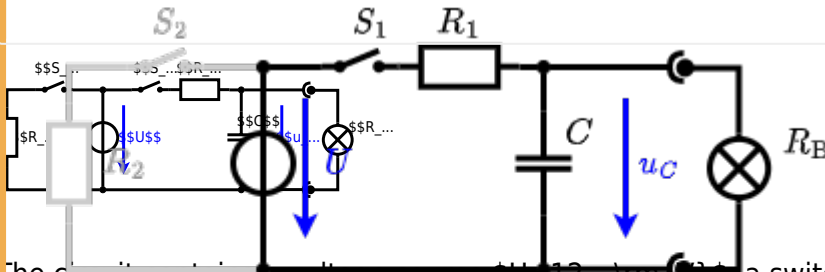
[electrical\\_engineering\\_and\\_electronics:task\\_6tqtqtue1e2nf2c7\\_with\\_calculation](#)  
 dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

### Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)

The capacitor becomes fully charged) dissipation of power in the circuit is again zero. The voltage across the capacitor is again \$0\$ at the moment \$t\_0=0\$ when the switch \$S\_1\$ is closed. Calculate the voltage \$u\_c(t\_2)\$ across the capacitor at \$t\_2=1\$ ms after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from \$U\$, \$R\_1\$, and \$R\_B\$.

The internal voltage of the equivalent source is \$U\_{eq} = U \cdot \frac{R\_B}{R\_1 + R\_B} = 12 \text{ V} \cdot \frac{12 \Omega}{20 \Omega + 12 \Omega} = 4.8 \text{ V}\$. The internal resistance is given by substituting the ideal voltage source is again short-circuiting \$R\_2\$.



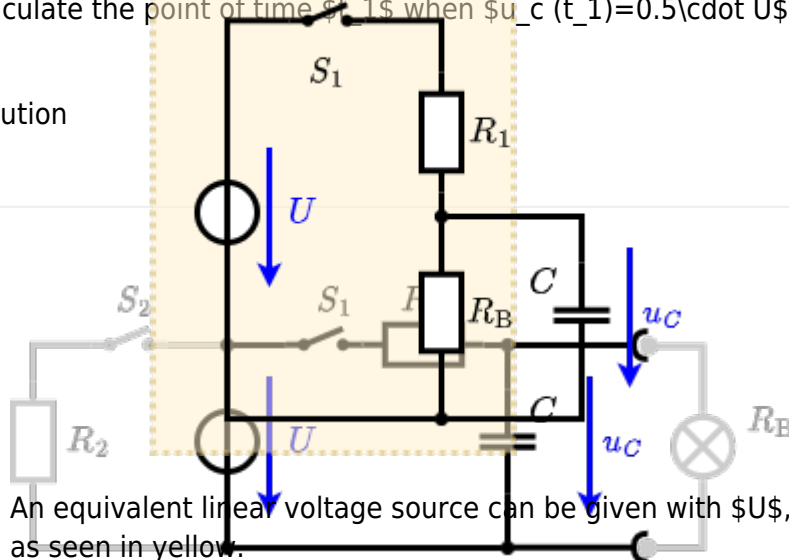
The circuit contains a voltage source \$U=12\$ V, a switch \$S\_1\$, a resistor of \$R\_1=20\$ Ohm and a capacitor of \$C=100\$ uF.

The switch \$S\_2\$ to an additional consumer \$R\_2\$ will be considered to be open for the first tasks. At the moment \$t\_0=0\$ the switch \$S\_1\$ is closed, the voltage across the capacitor is \$u\_c(t\_0)=0\$ V.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time \$t\_1\$ when \$u\_c(t\_1)=0.5 \cdot U\$.

Solution



An equivalent linear voltage source can be given with \$U\$, \$R\_1\$, and \$R\_B\$ as seen in yellow.

Therefore the voltage of the equivalent source is \$U\_{eq} = U \cdot \frac{R\_B}{R\_1 + R\_B} = 1/2 \cdot U\$. The internal resistance is given

by the following formula describing the time course of \$u\_c(t)\$ which has to be \$u\_c(t) = U\_{eq} \cdot (1 - e^{-t/\tau})\$. It has to be rearranged to \$1 - e^{-t/\tau} = 0.5 \cdot U\$. It follows \$e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R\_1 \cdot C \cdot \ln(2) \approx 14 \text{ ms}\$.

$$\frac{1}{2} \cdot U \cdot (1 - e^{-\frac{1}{\tau}}) \cdot I \cdot \mu F$$

electrical\_engineering\_and\_electronics:task\_tb6pi8dgh0m2e2pw\_with\_calculation charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

**Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the effective value of the current  $i(t)$  and the effective value of the voltage  $u(t)$ . The results ( $I_{eff}$  and  $U_{eff}$ ) shall be given.

After analysis, the following complex impedances can be extracted and brought into phase:  $Z_1 = (2 - j) \Omega$ ,  $Z_2 = (4 + j) \Omega$ ,  $Z_3 = (5 + j) \Omega$

.. Calculate the physical values of the two components.  
 Solution: 
$$I_{eff} = \frac{1}{\sqrt{2}} \sqrt{I_{eff}^2} = \frac{1}{\sqrt{2}} \sqrt{4.68^2 + 3.4^2} = 3.70 A$$

Solution  

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} \parallel \&= \frac{50 \angle 0^\circ}{(2 - j) + (4 + j) + (5 + j)} = \frac{50 \angle 0^\circ}{11 + j} = 4.68 \angle -4.68^\circ A$$
  
 The effective value of the current is  $I_{eff} = 3.70 A$ .  
 The effective value of the voltage is  $U_{eff} = 30.4 V$ .  
 With the complex part comes the physical value  $i(t) = 3.70 \sqrt{2} \cos(\omega t - 4.68^\circ)$

The phase  $\varphi_i$  can be calculated as 
$$\varphi_i = \arctan \left( \frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})} \right) = \arctan \left( \frac{-0.24}{4.68} \right) = -2.9^\circ$$

electrical\_engineering\_and\_electronics:task\_jti0uzudcmg4u22t\_with\_calculation complex impedance, exam ee1 ws2022

**Exercise E9 Impedances at different Frequencies**

**(written test, approx. 18 % of a 60-minute written test, WS2022)**

2. A series circuit contains a resistor with  $R = 200 \Omega$  and a capacitor with  $C = 40 \text{ nF}$ . The voltage source is  $v(t) = 300 \sin(2\pi \cdot 4 \cdot 10^6 t)$  V. The current through the resistor is  $i(t) = 1.0 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi)$  A. Determine the value of  $\phi$ .

Solution

$$Z = R + j\omega C = 200 + j(4 \cdot 10^6) \cdot 40 \cdot 10^{-9} = 200 + j160 \Omega$$

$$\phi = \arctan\left(\frac{160}{200}\right) = 38.7^\circ$$

Result:  $\phi = 38.7^\circ$

A series circuit means that the current is constant on every component. The equivalent impedance for  $R$  and  $C$  combined is given by  $Z = R + j\omega C$ . The voltage across the resistor is  $v_R(t) = i(t) \cdot R = 1.0 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi) \cdot 200$  V. The voltage across the capacitor is  $v_C(t) = i(t) \cdot j\omega C = 1.0 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi) \cdot j160$  V. The total voltage is  $v(t) = v_R(t) + v_C(t) = 200 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi) + j160 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi)$  V. The magnitude of the total voltage is  $|v(t)| = \sqrt{200^2 + 160^2} \cos(2\pi \cdot 4 \cdot 10^6 t - \phi) = 260 \cos(2\pi \cdot 4 \cdot 10^6 t - \phi)$  V. The phase angle  $\phi$  is determined by  $\tan(\phi) = \frac{160}{200} = 0.8$ , so  $\phi = \arctan(0.8) = 38.7^\circ$ .

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**Exercise E1 Complex Impedance Circuit**

**(written test, approx. 15 % of a 60-minute written test, WS2022)**

1. Consider the circuit shown below. The voltage source is  $v(t) = 3.0 \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$  V. The resistor has a resistance of  $R = 10 \Omega$ . The inductor has an inductance of  $L = 30 \mu\text{H}$  and the capacitor has a capacitance of  $C = 0.22 \mu\text{F}$ . Determine the effective value of the current  $I_{\text{eff}}$  through the resistor.

Solution

$$Z = R + j\omega L - j\omega C = 10 + j(2\pi \cdot 15 \cdot 10^3) \cdot 30 \cdot 10^{-6} - j(2\pi \cdot 15 \cdot 10^3) \cdot 0.22 \cdot 10^{-6}$$

$$Z = 10 + j1.884 - j0.207 = 10 + j1.677 \Omega$$

$$|Z| = \sqrt{10^2 + 1.677^2} = 10.13 \Omega$$

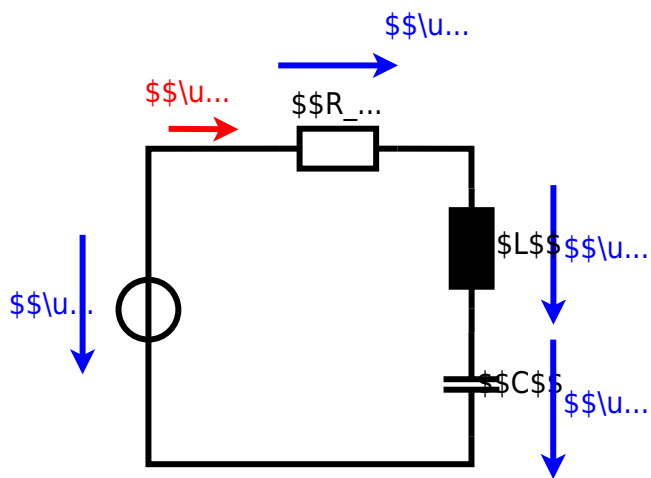
$$I_{\text{eff}} = \frac{V_{\text{eff}}}{|Z|} = \frac{3.0}{10.13} = 0.296 \text{ A}$$

Result:  $I_{\text{eff}} = 0.296 \text{ A}$

Draw the circuit diagram of the given circuit. Label all components, voltages, and currents.







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