

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

Exercise E9 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

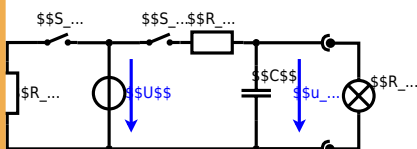
The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is open and the voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Resolution

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

Solution: The internal voltage source is $U_{int} = U \cdot \frac{R_2}{R_1 + R_2}$ and the internal resistance is $R_{int} = \frac{R_1 \cdot R_2}{R_1 + R_2}$.

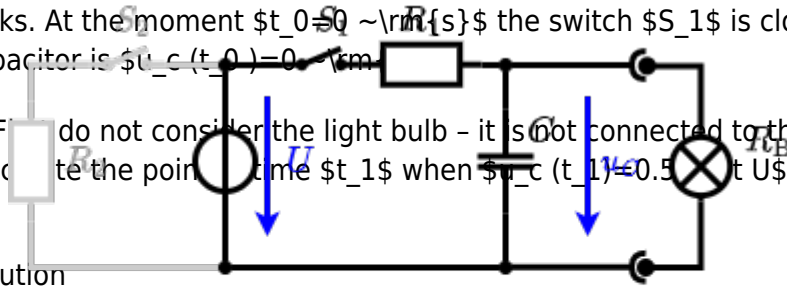
On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



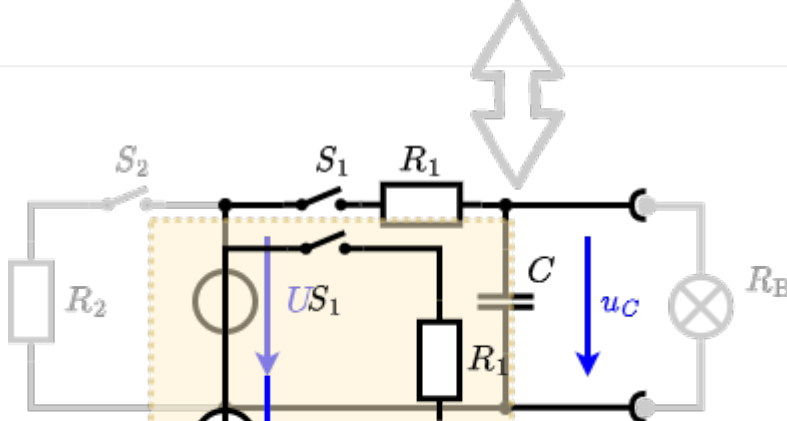
The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution



So, here only U and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ } \Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10 \text{ } \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ } \Omega \cdot 100 \text{ } \mu\text{F})})$$

Exercise E13 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A AC circuit with the resistor values $R_1 = 1 \text{ } \Omega$, $R_2 = 1 \text{ } \Omega$, $R_3 = 1 \text{ } \Omega$, $R_4 = 1 \text{ } \Omega$, $R_5 = 1 \text{ } \Omega$, $R_6 = 1 \text{ } \Omega$, $R_7 = 1 \text{ } \Omega$, $R_8 = 1 \text{ } \Omega$, $R_9 = 1 \text{ } \Omega$, $R_{10} = 1 \text{ } \Omega$, $R_{11} = 1 \text{ } \Omega$, $R_{12} = 1 \text{ } \Omega$, $R_{13} = 1 \text{ } \Omega$, $R_{14} = 1 \text{ } \Omega$, $R_{15} = 1 \text{ } \Omega$, $R_{16} = 1 \text{ } \Omega$, $R_{17} = 1 \text{ } \Omega$, $R_{18} = 1 \text{ } \Omega$, $R_{19} = 1 \text{ } \Omega$, $R_{20} = 1 \text{ } \Omega$, $R_{21} = 1 \text{ } \Omega$, $R_{22} = 1 \text{ } \Omega$, $R_{23} = 1 \text{ } \Omega$, $R_{24} = 1 \text{ } \Omega$, $R_{25} = 1 \text{ } \Omega$, $R_{26} = 1 \text{ } \Omega$, $R_{27} = 1 \text{ } \Omega$, $R_{28} = 1 \text{ } \Omega$, $R_{29} = 1 \text{ } \Omega$, $R_{30} = 1 \text{ } \Omega$, $R_{31} = 1 \text{ } \Omega$, $R_{32} = 1 \text{ } \Omega$, $R_{33} = 1 \text{ } \Omega$, $R_{34} = 1 \text{ } \Omega$, $R_{35} = 1 \text{ } \Omega$, $R_{36} = 1 \text{ } \Omega$, $R_{37} = 1 \text{ } \Omega$, $R_{38} = 1 \text{ } \Omega$, $R_{39} = 1 \text{ } \Omega$, $R_{40} = 1 \text{ } \Omega$, $R_{41} = 1 \text{ } \Omega$, $R_{42} = 1 \text{ } \Omega$, $R_{43} = 1 \text{ } \Omega$, $R_{44} = 1 \text{ } \Omega$, $R_{45} = 1 \text{ } \Omega$, $R_{46} = 1 \text{ } \Omega$, $R_{47} = 1 \text{ } \Omega$, $R_{48} = 1 \text{ } \Omega$, $R_{49} = 1 \text{ } \Omega$, $R_{50} = 1 \text{ } \Omega$, $R_{51} = 1 \text{ } \Omega$, $R_{52} = 1 \text{ } \Omega$, $R_{53} = 1 \text{ } \Omega$, $R_{54} = 1 \text{ } \Omega$, $R_{55} = 1 \text{ } \Omega$, $R_{56} = 1 \text{ } \Omega$, $R_{57} = 1 \text{ } \Omega$, $R_{58} = 1 \text{ } \Omega$, $R_{59} = 1 \text{ } \Omega$, $R_{60} = 1 \text{ } \Omega$, $R_{61} = 1 \text{ } \Omega$, $R_{62} = 1 \text{ } \Omega$, $R_{63} = 1 \text{ } \Omega$, $R_{64} = 1 \text{ } \Omega$, $R_{65} = 1 \text{ } \Omega$, $R_{66} = 1 \text{ } \Omega$, $R_{67} = 1 \text{ } \Omega$, $R_{68} = 1 \text{ } \Omega$, $R_{69} = 1 \text{ } \Omega$, $R_{70} = 1 \text{ } \Omega$, $R_{71} = 1 \text{ } \Omega$, $R_{72} = 1 \text{ } \Omega$, $R_{73} = 1 \text{ } \Omega$, $R_{74} = 1 \text{ } \Omega$, $R_{75} = 1 \text{ } \Omega$, $R_{76} = 1 \text{ } \Omega$, $R_{77} = 1 \text{ } \Omega$, $R_{78} = 1 \text{ } \Omega$, $R_{79} = 1 \text{ } \Omega$, $R_{80} = 1 \text{ } \Omega$, $R_{81} = 1 \text{ } \Omega$, $R_{82} = 1 \text{ } \Omega$, $R_{83} = 1 \text{ } \Omega$, $R_{84} = 1 \text{ } \Omega$, $R_{85} = 1 \text{ } \Omega$, $R_{86} = 1 \text{ } \Omega$, $R_{87} = 1 \text{ } \Omega$, $R_{88} = 1 \text{ } \Omega$, $R_{89} = 1 \text{ } \Omega$, $R_{90} = 1 \text{ } \Omega$, $R_{91} = 1 \text{ } \Omega$, $R_{92} = 1 \text{ } \Omega$, $R_{93} = 1 \text{ } \Omega$, $R_{94} = 1 \text{ } \Omega$, $R_{95} = 1 \text{ } \Omega$, $R_{96} = 1 \text{ } \Omega$, $R_{97} = 1 \text{ } \Omega$, $R_{98} = 1 \text{ } \Omega$, $R_{99} = 1 \text{ } \Omega$, $R_{100} = 1 \text{ } \Omega$.
 Result: $I_B = 20 \text{ mA}$, $I_C = 40 \text{ mA}$, $I_D = 50 \text{ mA}$, $I_E = 30 \text{ mA}$, $I_F = 10 \text{ mA}$.
 A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on R_3 and C_3 .

$$\underline{U} = \underline{U}_R + \underline{U}_C$$

$$\underline{U} = \underline{I} R_3 + \underline{I} X_C$$

So it gets clear that perpendicular components can be summed over $\sqrt{}$ (Pythagoras). It is noted, since R_3 is 30Ω and X_C is 40Ω .

Therefore the resulting current of the parallel circuit is given as:

$$I = \sqrt{I_R^2 + I_C^2}$$

$$I = \sqrt{\left(\frac{U}{30}\right)^2 + \left(\frac{U}{40}\right)^2}$$

This can be rearranged to get R_{eq} :

$$R_{eq} = \frac{U}{I} = \frac{U}{\sqrt{\left(\frac{U}{30}\right)^2 + \left(\frac{U}{40}\right)^2}}$$

Back to the first formula:

$$U = I R_3 + I X_C$$

$$U = I \left(R_3 + X_C \right)$$

Exercise E11 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle and the effective value of the current through the components (R and X_L) shall be given.

After analysis, the following formula can be extracted and brought into phase form:

$$\underline{U} = \underline{I} (R + j\omega L)$$

Solution

.. Calculation of the physical values of the components.

$$R = 10 \Omega$$

$$X_L = \omega L = 2\pi \cdot 50 \cdot 0.02 = 6.28 \Omega$$

Solution

$$\underline{U} = \underline{I} (R + j\omega L)$$

The current and voltage are in phase since the Z is real.

resulting $I = \frac{U}{Z} = \frac{50}{10 + j6.28} = 4.68 - j2.98$

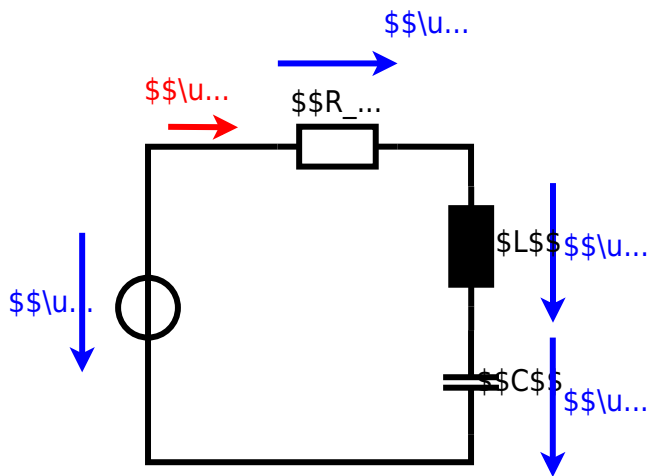
Therefore, the component R is in phase with the ω and the X_L is 90° ahead.

$$I = \frac{50}{\sqrt{10^2 + 6.28^2}} = 4.68 - j2.98$$

$$I = 5.5 \angle -33.7^\circ$$

The phase angle φ can be calculated as:

$$\varphi = \arctan\left(\frac{\text{Im}()}{\text{Re}()}\right) = \arctan\left(\frac{-2.98}{4.68}\right) = -33.7^\circ$$



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