

Exam Winter Semester 2022

Student Group

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Exam Summer Semester 2021

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

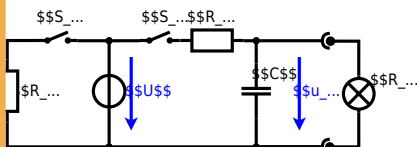
Exercise E9 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is closed and the capacitor is fully charged. At $t = 0$ the switch S_1 is opened and the switch S_2 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

Solution: The circuit can be simplified to an equivalent circuit. The voltage source is $U_{eq} = U \cdot \frac{R_2}{R_1 + R_2}$ and the internal resistance is $R_{eq} = \frac{R_1 \cdot R_2}{R_1 + R_2}$. On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on R_3 and C_3 .

Equivalent impedance for R_3 and C_3 is $Z_{RC} = R_3 + \frac{1}{j\omega C_3}$

So it gets legs that perpendicular legs that can be simplified to $Z_{RC} = \frac{R_3 + j\omega R_3^2 C_3}{1 + \omega^2 R_3^2 C_3^2}$

Therefore the resulting current of the parallel circuit is given as:

$$I_{RC} = \frac{U}{Z_{RC}} = \frac{U}{R_3 + \frac{1}{j\omega C_3}} = \frac{U}{R_3 + j\omega R_3^2 C_3}$$

This can be rearranged to get $Z_{RC} = \frac{R_3 + j\omega R_3^2 C_3}{1 + \omega^2 R_3^2 C_3^2}$

Back to the first formula $I = \frac{U}{Z_{RC}}$

$$I = \frac{U}{R_3 + \frac{1}{j\omega C_3}} = \frac{U}{R_3 + j\omega R_3^2 C_3}$$

Exercise E11 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle of the circuit (Figure 1) at $\omega = 300 \text{ rad/s}$. Both R and C are in the components. (R and X_L) shall be given.

After analysis, the full bridge form of the circuit impedance is extracted and given in phase form $Z = |Z| \angle \theta = |Z| (\cos \theta + j \sin \theta)$

Solution

.. Calculation of physical values of the components.

Solution

$$R = 10 \text{ } \Omega$$

Solution

The current and voltage are in phase since there is only a pure resistor (50 real) resulting in $\theta = 0^\circ$

Therefore, the component $4.68 \text{ } \Omega$ is in phase with the $50 \text{ } \Omega$ resistor.

$$Z_{RC} = R_3 + \frac{1}{j\omega C_3} = 10 + \frac{1}{j300 \cdot 0.0001} = 10 - j3.33$$

$$Z_{total} = 50 + 10 - j3.33 = 60 - j3.33$$

The phase angle θ is calculated as:

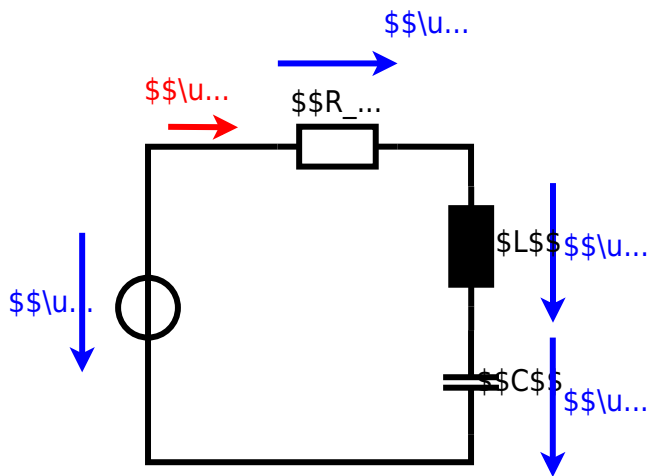
$$\theta = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-3.33}{60}\right) = -3.16^\circ$$

With the complex part comes the complex value $Z = |Z| \angle \theta$

$$|Z| = \sqrt{60^2 + 3.33^2} = 60.18 \text{ } \Omega$$

The phase angle θ can be calculated as:

$$\theta = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-3.33}{60}\right) = -3.16^\circ$$



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