

Exam Winter Semester 2022

Student Group

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Exam Summer Semester 2021

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

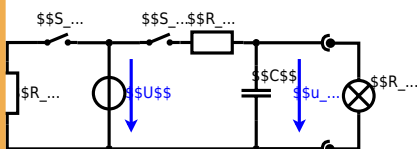
Exercise E1 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is open and the voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

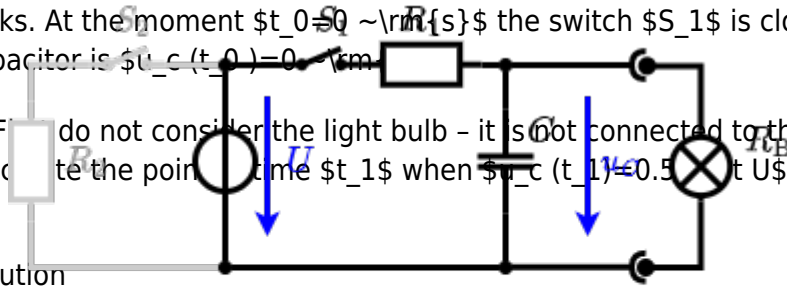
Solution: The internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



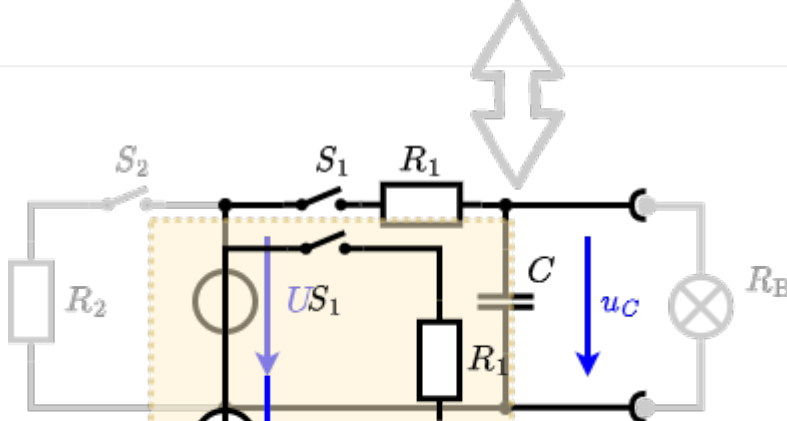
The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution



So, here only U and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ } \Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10 \text{ } \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ } \Omega \cdot 100 \text{ } \mu\text{F})})$$

Exercise E9 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC circuit with resistor values $R_1 = 1 \text{ } \Omega$ and $R_2 = 1 \text{ } \Omega$, and a capacitor with $C = 1 \text{ } \mu\text{F}$ is shown in the following circuit (of 3S) $U = 1 \text{ V}$.
 Result: $f_1 = 20 \text{ kHz}$ (high-pass filter) $Z_1 = 1 \text{ } \Omega$ through R_1 .
 R_2 resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on every component.

Equivalent impedance for voltage is the same as R_{eq} and Z_{eq} .

$$\underline{U} = \underline{I} \cdot \underline{Z} = \underline{I} \cdot (R_1 + j\omega L + \frac{1}{j\omega C})$$

So it gets clear that perpendicular components can be summed over $\sqrt{R^2 + (X_L - X_C)^2}$ instead, since R is $\sqrt{R^2 + (X_L - X_C)^2}$.

Therefore the resulting current of the parallel circuit is given as:

$$I = \frac{U}{\sqrt{R^2 + (X_L - X_C)^2}}$$

This can be rearranged to get R_{eq} :

$$R_{eq} = \sqrt{\left(\frac{U}{I}\right)^2 - (X_L - X_C)^2}$$

Back to the first formula:

$$I = \frac{U}{\sqrt{R^2 + (X_L - X_C)^2}}$$

Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

1. Calculate the phase angle and the effective value of the current through the components. (R and X_L) shall be given.

After analysis, the full bidirectional impedance value is extracted and given in phase (angle) $Z = (20 + j4) \Omega$.

Solution

.. Calculation of physical values of the components.

$$R = \frac{U}{I} \cos(\phi) = \frac{10}{0.17} \cos(26.1^\circ) = 87.06 \Omega$$

Solution

The current and voltage are in phase since the impedance is purely real resulting in $\phi = 0^\circ$.

Therefore, the component 4.68Ω is in phase with the 300 Hz voltage.

$$I = \frac{U}{Z} = \frac{10}{\sqrt{4.68^2 + (3.4 - 16)^2}} = 0.17 \text{ A}$$

The phase angle ϕ can be calculated as:

$$\phi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-12.6}{4.68}\right) = -69.1^\circ$$

With the complex part comes the complex value $Z = 4.68 - j12.6 \Omega$.

The phase angle ϕ can be calculated as:

$$\phi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-12.6}{4.68}\right) = -69.1^\circ$$

Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

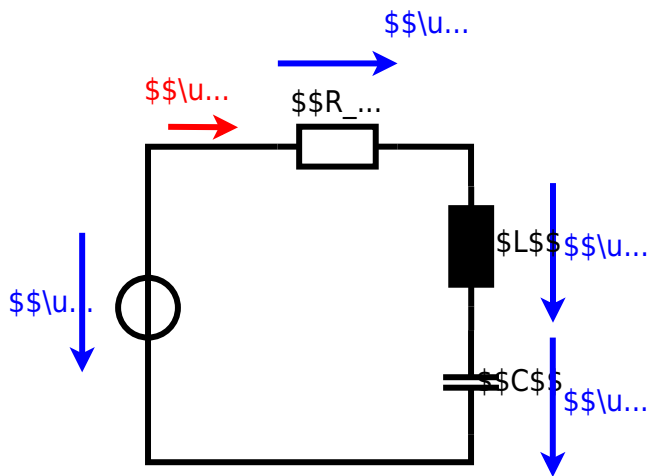
2. Calculate the complex impedance Z , the magnitude $|Z|$, and the phase ϕ of the circuit. The voltage source is $u(t) = 3.0 \cdot \sin(2\pi \cdot 15 \cdot t)$ V. The circuit consists of a resistor of $R = 10 \text{ k}\Omega$, an inductor of $L = 30 \text{ }\mu\text{H}$, and a capacitor of $C = 0.22 \text{ }\mu\text{F}$, all in series.

Result

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\begin{align*} Z &= R + j\omega L - j\omega C = 10 \text{ k}\Omega + j48.2 \text{ }\Omega - j19.8 \text{ }\Omega \\ \end{align*}
\begin{align*} |Z| &= \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{10^2 + (48.2 - 19.8)^2} \text{ k}\Omega \\ \phi &= \arctan\left(\frac{X_L - X_C}{R}\right) = \arctan\left(\frac{48.2 - 19.8}{10}\right) \text{ rad} \\ \end{align*}
\begin{align*} Z &= 10 \text{ k}\Omega + j28.4 \text{ }\Omega \\ |Z| &= 10.4 \text{ k}\Omega \\ \phi &= 1.5 \text{ rad} \\ \end{align*}
\begin{align*} \underline{Z} &= R + jZ_L - jZ_C \\ &= R + j\omega L - j\omega C \\ &= 10 \text{ k}\Omega + j(2\pi \cdot 15 \cdot 30 \cdot 10^{-6}) - j(2\pi \cdot 15 \cdot 0.22 \cdot 10^{-6}) \\ &= 10 \text{ k}\Omega + j28.4 \text{ }\Omega - j19.8 \text{ }\Omega \\ &= 10 \text{ k}\Omega + j8.6 \text{ }\Omega \\ \end{align*}
\begin{align*} |Z| &= \sqrt{R^2 + (Z_L - Z_C)^2} \\ &= \sqrt{10^2 + (8.6)^2} \text{ k}\Omega \\ &= 10.4 \text{ k}\Omega \\ \end{align*}
\begin{align*} \phi &= \arctan\left(\frac{Z_L - Z_C}{R}\right) \\ &= \arctan\left(\frac{8.6}{10}\right) \text{ rad} \\ &= 0.7 \text{ rad} \\ \end{align*}

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