

Exam Winter Semester 2022

Student Group

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Exam Summer Semester 2021

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

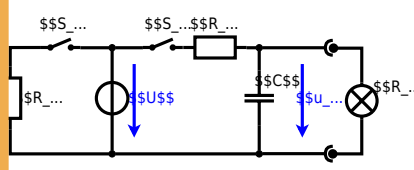
Exercise E9 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is open and the voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

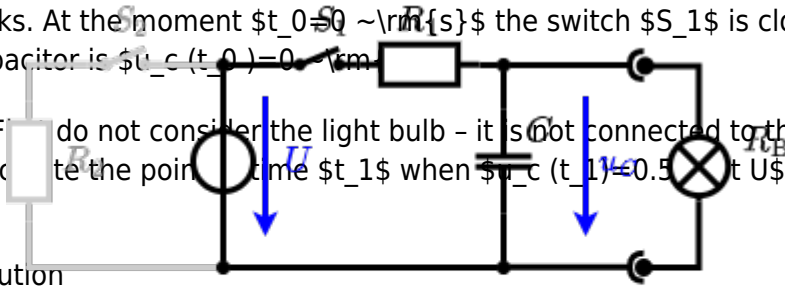
Solution: The ideal voltage source U is in series with the resistor R_1 and the resistor R_2 is in parallel with the capacitor. On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



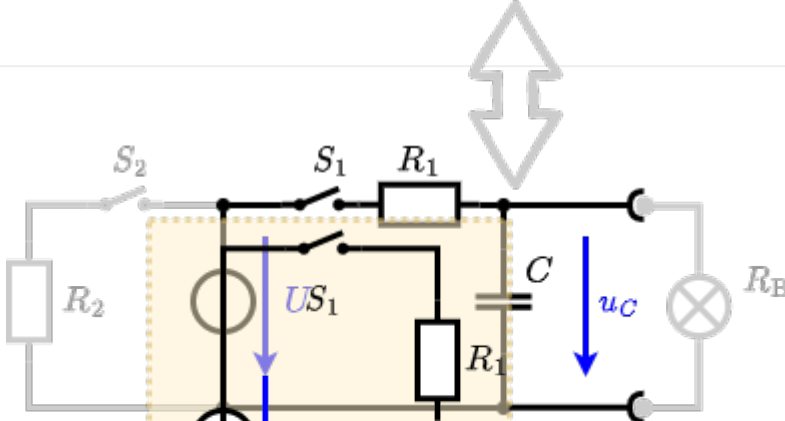
The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution



So, here only U and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ } \Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10 \text{ } \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ } \Omega \cdot 100 \text{ } \mu\text{F})})$$

Exercise E13 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC circuit with resistor values $R_1 = 1 \text{ } \Omega$ and $R_2 = 3 \text{ } \Omega$ is shown in the following circuit (of 3S) $U = 1.0 \text{ V}$.
 Result: $f = 20 = 450 \text{ kHz}$ Hz higher generates a current $I = 50 \text{ mA}$ through R_1 .
 A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on R_3 and C_3 .

$$\underline{U} = \underline{U}_R + \underline{U}_C$$

$$\underline{U} = \underline{I} R_3 + \underline{I} X_C$$

So it gets clear that perpendicular components can be summed over $\sqrt{R_3^2 + X_C^2}$ instead, since R_3 is $\sqrt{R_3^2 + X_C^2} \cdot \sin(\phi)$ and X_C is $\sqrt{R_3^2 + X_C^2} \cdot \cos(\phi)$.

Therefore the resulting current of the parallel circuit is given as:

$$I = \frac{U}{\sqrt{R_3^2 + X_C^2}}$$

This can be rearranged to get R_3 :

$$R_3 = \frac{U}{I} \sqrt{1 - \left(\frac{X_C}{U/I}\right)^2}$$

Back to the first formula:

$$I = \frac{U}{\sqrt{R_3^2 + X_C^2}}$$

Exercise E11 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle and the current I if $U = 50 \text{ V}$, $R = 10 \text{ }\Omega$, $X_L = 10 \text{ }\Omega$, $X_C = 20 \text{ }\Omega$ and $f = 50 \text{ Hz}$.

Result: After analysis, the full bridge circuit can be simplified to a series circuit in phase. $Z = 10 + j10 - j20 = 10 - j10 \text{ }\Omega$.

Solution

1. Calculation of the real values of the components.

$$R = 10 \text{ }\Omega$$

Solution

Solution

The current and voltage are in phase since Z is purely real. Resulting $I = \frac{U}{Z} = \frac{50}{10 - j10} = 4.68 \text{ A}$.

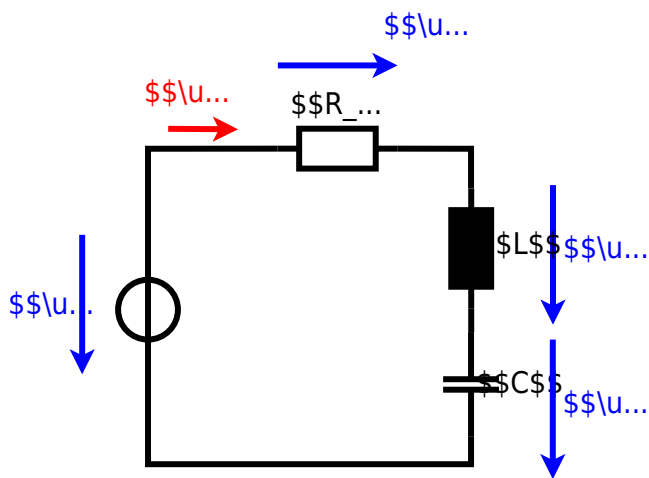
Therefore, the component R is in phase with the voltage U . $X_L = j10 \text{ }\Omega$ and $X_C = -j20 \text{ }\Omega$ are in phase with I .

With the complex part comes the phase angle ϕ .

$$\phi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{-10}{10}\right) = -45^\circ$$

The phase angle ϕ can be calculated as:

$$\phi = \arctan\left(\frac{-4.68 \text{ }\Omega}{0.24 \text{ }\Omega}\right)$$



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